

Audio Special Effects

Professor Deepa Kundur

University of Toronto

Audio Effects

▶ **Q:** What is an **audio effect**?

▶ **A:** artificially enhanced **sound** or **sound processes** used to emphasize **artistic** content in films, television, shows, live performance, animation, video, games, music or other media.

Common Audio Special Effects

Two common types:

- ▶ **Delay-based special effects**
 - ▶ simple echo
 - ▶ reverberation
 - ▶ flanging
 - ▶ chorus
- ▶ **Rate-conversion special effects**
 - ▶ downsampling (decimation)
 - ▶ upsampling
 - ▶ voice gender changers

Delay-Based Special Effects

Delay Effects

- ▶ **Q:** What is a **delay effect**?
 - ▶ **A:** audio effect which records an input signal to an audio **storage** medium and then **plays it back** (possibly multiple times) into the recording again to create the sound of a repeating **decaying echo**.

- ▶ **Q:** What is this so popular?
 - ▶ **A:** easy to achieve even before the use of computers while adding an attractive texture to the music.

Analog and Digital Delays

- ▶ Analog delay
 - ▶ created by recording in a naturally **reverberant space**
 - ▶ achieved using **tape loops** improvised on reel-to-reel magnetic recording systems
 - ▶ signal is **recorded** on analog tape and **played back from same piece of tape** through the use of two different record and replay heads
 - ▶ adjusting loop length and distance between the read and write heads enables control over delayed echo

- ▶ Digital delay
 - ▶ first introduced in 1984 by Boss Corporation
 - ▶ provides great flexibility, portability and programmability

Examples of Delay Effects

Delay-based special effects:

- ▶ simple echo
- ▶ reverberation
- ▶ flanging
- ▶ chorus

Note: Check out course website on Handouts page for an example of a simple echo.

Single Echo

- ▶ **Q:** How can we achieve a single echo from a given sound signal $x(n)$?
 - ▶ **A:** add a **delayed** and **attenuated** version of $x(n)$ to itself.

$$y(n) = x(n) + \alpha x(n - n_0)$$

Note: The audio example available on the course web page was generated using $\alpha = 0.35$ and $n_0 = 20000$ with $F_s = 44\text{kHz}$. Thus the echo delay is $20000/44000 = 0.45$ sec.

Single Echo

- ▶ **Q:** How can we characterize this single echo generation system?
Hint: The system is linear time-invariant?

- ▶ **A:** impulse response and frequency response.

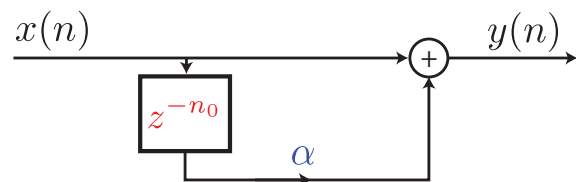
Single Echo: Impulse Response

$$y(n) = x(n) + \alpha x(n - n_0)$$

Let $x(n) = \delta(n)$ to give $y(n) = h(n)$.

$$\therefore h(n) = \delta(n) + \alpha \delta(n - n_0).$$

Single Echo: Filter Implementation



LTI Single-zero system

Note: This is also called a delay line in audio applications and is characterized by n_0 and α .

Single Echo: Frequency Response

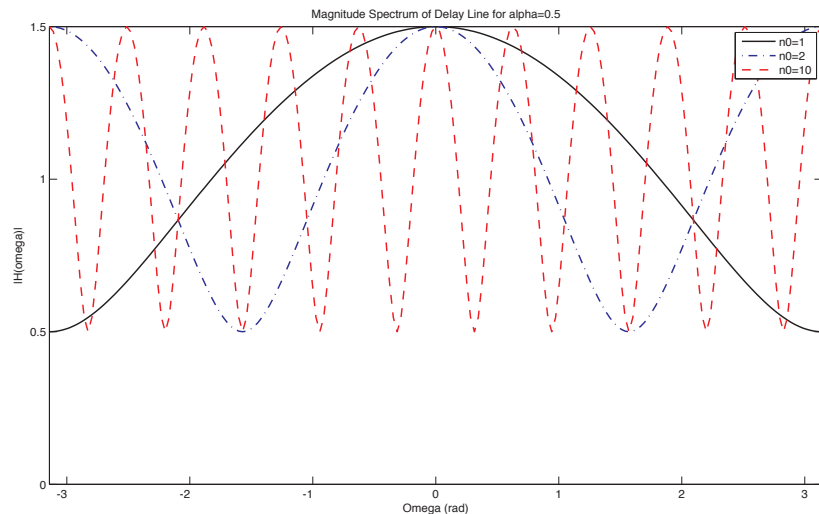
$$h(n) = \delta(n) + \alpha \delta(n - n_0) \quad \text{FIR system}$$

$$\begin{aligned} H(\omega) &= \sum_{n=-\infty}^{\infty} h(n) e^{-j\omega n} \\ &= \sum_{n=-\infty}^{\infty} [\delta(n) + \alpha \delta(n - n_0)] e^{-j\omega n} = 1 + \alpha e^{-j\omega n_0} \\ |H(\omega)| &= \sqrt{1 + \alpha^2 + 2\alpha \cos(\omega n_0)} \end{aligned}$$

Note: $1 - \alpha \leq |H(\omega)| \leq 1 + \alpha$.

Single Echo: Frequency Response

Note: $1 - \alpha \leq |H(\omega)| \leq 1 + \alpha$; $\alpha = 0.5$ in example.



Extended Echo: Impulse Response

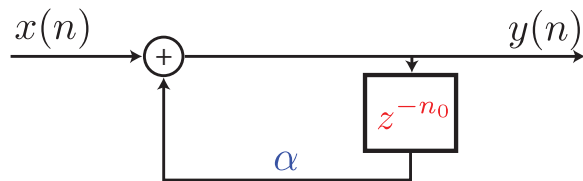
Consider an infinite series of echos geometrically decaying in amplitude and with equally spaced delays:

$$y(n) = x(n) + \alpha x(n - n_0) + \alpha^2 x(n - 2n_0) + \dots$$

Let $x(n) = \delta(n)$ to give $y(n) = h(n)$.

$$\begin{aligned} \therefore h(n) &= \delta(n) + \alpha \delta(n - n_0) + \alpha^2 \delta(n - 2n_0) + \dots \\ &= \sum_{k=0}^{\infty} \alpha^k \delta(n - kn_0) \end{aligned}$$

Extended Echo: Filter Implementation



LTI Single-pole system

Extended Echo: Frequency Response

$$h(n) = \sum_{k=0}^{\infty} \alpha^k \delta(n - kn_0) \quad \text{IIR system}$$

$$\begin{aligned} H(\omega) &= \sum_{n=-\infty}^{\infty} h(n) e^{-j\omega n} \\ &= \sum_{n=-\infty}^{\infty} \left[\sum_{k=0}^{\infty} \alpha^k \delta(n - kn_0) \right] e^{-j\omega n} \\ &= \sum_{k=0}^{\infty} \sum_{n=-\infty}^{\infty} \alpha^k e^{-j\omega n} \delta(n - kn_0) \\ &= \sum_{k=0}^{\infty} \alpha^k e^{-j\omega kn_0} = \sum_{k=0}^{\infty} (\alpha e^{-j\omega n_0})^k = \frac{1}{1 - (\alpha e^{-j\omega n_0})} \end{aligned}$$

for $|\alpha| < 1$. Instability occurs for $\alpha > 1$.

Extended Echo as Reverberation

- ▶ Consider an original sound source $x(n)$ of finite duration in the order of a few seconds.
- ▶ Specifically, let its time duration be T_d sec and its sample duration be $N_d = \lfloor \frac{T_d}{T} \rfloor = \lfloor T_d \cdot F_s \rfloor$ samples.
- ▶ Let the echo generation parameters be $|\alpha| < 1$ and n_0 “small” such that

$$n_0 \cdot T = \frac{n_0}{F_s} \ll 1 \quad (\text{normally in the order of } 0.01 - 1 \text{ msec})$$

Extended Echo as Reverberation

- ▶ When the original sound source is present, the echoes overlap first building up the overall sound effect.
 - ▶ For a source that is T_d sec in duration,

$$\text{No. Overlapping Echoes} = \left\lfloor T_d \frac{F_s}{n_0} \right\rfloor = \left\lfloor \frac{N_d}{n_0} \right\rfloor \gg 1$$

- ▶ After the original source has stopped, the overall sound decays due to the echo reflections that eventually die out due to $\alpha < 1$; sounds like you are in a **music hall**.

This overall process is a type of reverberation.

Reverberation

Good examples at:

<http://www.youtube.com/watch?v=cGBn7sU6m3k>

Reverberation

Recall,

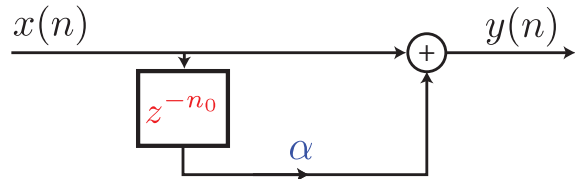
- ▶ First the echoes overlap with the original source signal building up the sound effect.
- ▶ When the original source has stopped, the sound may temporarily persist and then eventually die out.

There are other ways to achieve a “richer” reverberation than our prior example ...

Reverberation

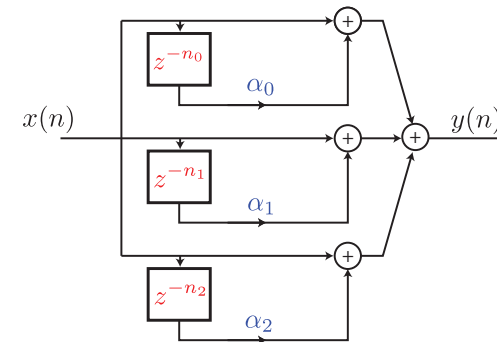
Example: More realistic reverb using multiple delay lines

- ▶ Use multiple **delay lines** with delays that are relatively prime, so that the echoes emanating from each lines do not ever overlap giving a richer sound.
- ▶ Single **delay line**:



Reverberation

Three delay line example:

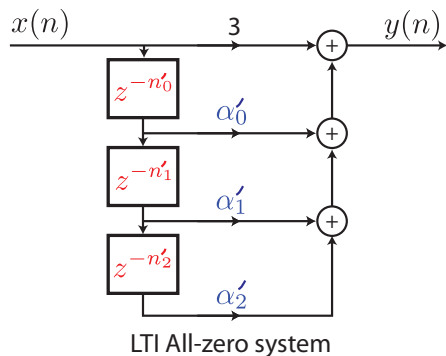


where

- ▶ $n_0 > n_1 > n_2$ are relatively prime

Reverberation

Note: the three delay line is equivalent to the following:



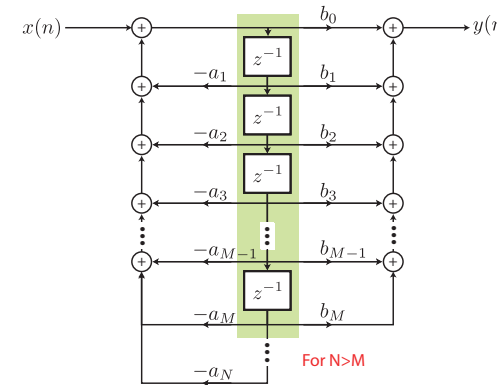
where

- ▶ $\alpha_i = \alpha'_i$ for $i = 0, 1, 2$
- ▶ $n'_0 = n_0$
- ▶ $n'_1 = n_1 - n_0$
- ▶ $n'_2 = n_2 - n_1 - n_0$

LTI All-zero system

Reverberation

For a more realistic reverb:



where

- ▶ feedforward and feedback present
- ▶ poles and zeros provide a more all-pass spectrum for realism
- ▶ more parameters to tune or experimentally estimate

Flanging

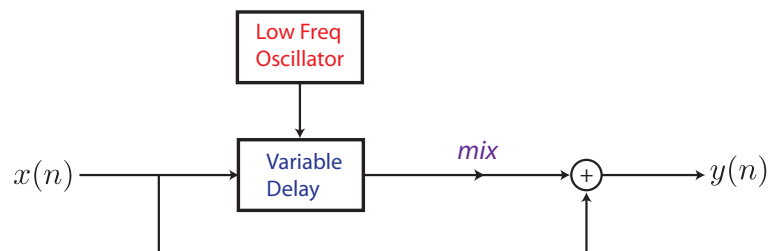
- ▶ process of **mixing** two signal together that are nearly identical such that one signal is a **slightly variably** delayed version of the other
- ▶ manifests like a “swooshing” sound
- ▶ a variation of this sound often occurs when instruments are trying to tune to a tuning fork

Flanging

Good examples at:

http://www.youtube.com/watch?v=NAqQvs_WXs8&feature=related

Flanging



- ▶ The **low frequency oscillator (LFO)** controls the **delay** of $x(n)$ which may change from block to block or even sample to sample.
- ▶ The scalar constant **mix** determines the proportion of the delayed signal that is added back to the original source.

Flanging

- ▶ Let $d(n)$ be the variable delay for $x(n)$ controlled by the **LFO**.
- ▶ Let the **LFO** provide the following sinusoidal signal:

$$\begin{aligned}
 d(n) &= \text{round}(\alpha \sin(2\pi f_0 n) + \beta) \\
 y(n) &= x(n) + \text{mix} \cdot x(n + d(n)) \\
 &= x(n) + \text{mix} \cdot x(n + \text{round}(\alpha \sin(2\pi f_0 n) + \beta))
 \end{aligned}$$

Flanging

$$y(n) = x(n) + \text{mix} \cdot x(n + \text{round}(\alpha \sin(2\pi f_0 n) + \beta))$$

- ▶ rate is given by f_0 and is generally small; typically $f_0 \cdot F_s$ should be 0.7 Hz (classical flange sound) up to 6 Hz (slight whammy effect) or even 20 Hz (mechanistic warble effect).
- ▶ sweep depth is given by 2α ; α should be selected so that the temporal (i.e., refers to seconds not samples) sweep depth is around a couple of milliseconds.
- ▶ delay is given by $\beta - \alpha$ and represents the minimum delay reached by the LFO; typically β should be set so that the delay is 1-10 milliseconds; note: human ear will perceive an echo (not flange) if the delay is more than 50-70 milliseconds!

Flanging: Instantaneous "Frequency Response"

Consider fixed delay n_0 and $\text{mix} = 1$:

$$y(n) = x(n) + x(n - n_0)$$

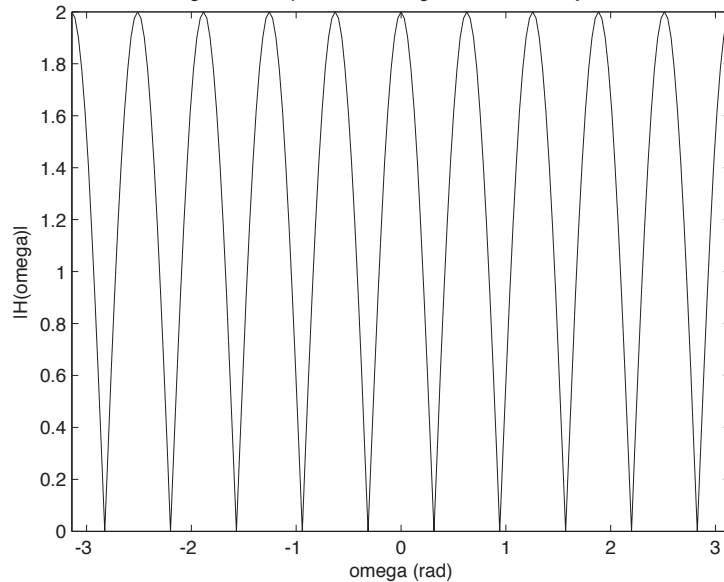
$$Y(\omega) = X(\omega) + e^{-j\omega n_0} X(\omega)$$

$$H(\omega) = \frac{Y(\omega)}{X(\omega)} = 1 + e^{-j\omega n_0}$$

$$= 2e^{-j\omega n_0/2} \cos(\omega n_0/2)$$

$$\therefore |H(\omega)| = 2|\cos(\omega n_0/2)|$$

"Magnitude Response" for Flange with Fixed Delay, $n_0=10$

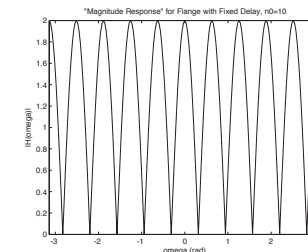


- ▶ spectrum nulls occur when argument of the cosine is an **odd** multiple of π :

$$\omega \frac{n_0}{2} = (2k + 1)\pi \quad \text{or} \quad \omega = \frac{2(2k + 1)\pi}{n_0}$$

for $k = 0, 1, 2, \dots$

- ▶ If the delay n_0 varies, then so do the spectrum nulls.



Flanging: Instantaneous “Frequency Response”

Thus, one can envision flanging as being the result of changing the position of the nulls of the frequency response.

A **cautionary note**: the flanging system is not LTI therefore, its frequency response does not fully characterize it, or we may say it has no frequency response!

Thus, this analysis is just a tool to intuitively explain the flange effect.

From Flange to Chorus

- ▶ Overall a classic flange has a delay ranging between **1 - 10** milliseconds.
- ▶ To create a chorus effect, this delay range must be between **30 - 50** milliseconds
- ▶ A delay above **50** milliseconds will be perceived as an echo.

Chorus

- ▶ A chorus effect sounds like more than one instrument is playing.
- ▶ Good examples at:

<http://www.youtube.com/watch?v=ZSL1w9UeSgc>

Rate-Conversion Special Effects

Rate-Conversion Special Effects

- ▶ Shifting, stretching and/or expanding spectral information across frequency bands can provide interesting effects especially for voice signals.
- ▶ Roughly speaking moving spectral content to lower frequencies adds base making a voice sound more male. Similarly, moving spectral content to higher frequency adds treble making a voice sound more female.
- ▶ One way to achieve spectral shifts, stretches and expansions is through **sampling rate conversion**.

Sampling Rate Conversion

Reference:

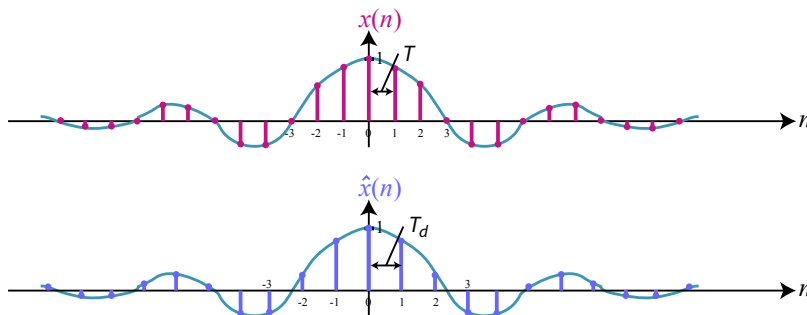
Sections 11.2, 11.3 and 11.4 of

John G. Proakis and Dimitris G. Manolakis, *Digital Signal Processing: Principles, Algorithms, and Applications*, 4th edition, 2007.

Sampling Rate Conversion

- ▶ **Goal:** Given a discrete-time signal $x(n)$ sampled at period T from an **underlying** continuous-time signal $x_a(t)$, determine a new sequence $\hat{x}(n)$ that is a sampled version of $x_a(t)$ at a different sampling rate T_d .

$$x(n) = x_a(nT) \quad \hat{x}(n) = x_a(nT_d)$$



Sampling Rate Conversion for Audio Effects

Two fundamental questions for use in audio effects applications:

- ▶ What does sampling rate conversion do to the frequency spectrum of a signal?
- ▶ How is it best to implement sampling rate conversion?

Sampling Rate Conversion

► One Interpretation:

1. Reconstruct the underlying continuous-time signal $x_a(t)$ from samples $x(n) = x_a(nT)$.
2. Resample at the desired sampling rate: $\hat{x}(n) = x_a(nT_d)$.

► If

$$\frac{T}{T_d} = \text{rational number}$$

then sampling rate conversion becomes equivalent to **sampling** and/or **interpolation** of discrete-time signals.

Sampling and Interpolation of Discrete-Time Signals

Let $D, I \in \{1, 2, 3, 4, \dots\}$

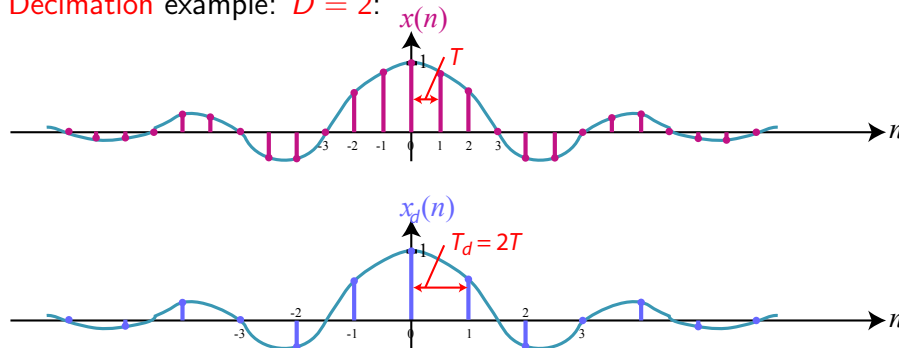
- For $T_d = DT$: called decimation or downsampling
- For $T_d = \frac{T}{I}$: called interpolation or upsampling

Sampling of Discrete-Time Signals

Suppose a discrete-time signal $x(n)$ is sampled by taking every D th sample as follows:

$$x_d(n) = x(nD), \quad \text{for all } n$$

Decimation example: $D = 2$:



Sampling of Discrete-Time Signals

Q: What happens to the signal spectrum during decimation?

Q: What is the relationship between $X(F)$ and $X_d(F)$?

Sampling of Discrete-Time Signals

Recall when we sample a continuous-time signal $x(t)$ to produce $x(n)$, we have the following relationships:

$$x(n) = x_a(nT) \xleftrightarrow{\mathcal{F}} X(F) = \frac{1}{T} \sum_{k=-\infty}^{\infty} X_a\left(F - \frac{k}{T}\right)$$

sampling $\xleftrightarrow{\mathcal{F}}$ periodic extension

Suppose

$$x_d(n) = x(nD) = x_a(\underbrace{nD}_T)$$

$$x(n) = x_a(nT)$$

$$x(n) = x_a(nT)$$

$$X(F) = \frac{1}{T} \sum_{k=-\infty}^{\infty} X_a\left(F - \frac{k}{T}\right)$$

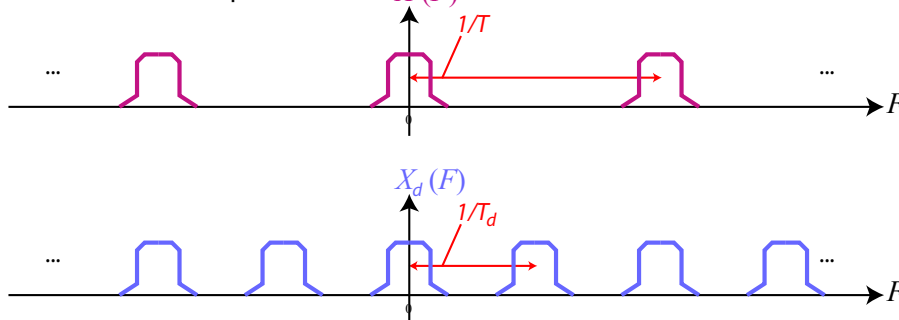
$$x_d(n) = x_a(nDT)$$

$$X_d(F) = \frac{1}{DT} \sum_{k=-\infty}^{\infty} X_a\left(F - \frac{k}{DT}\right)$$

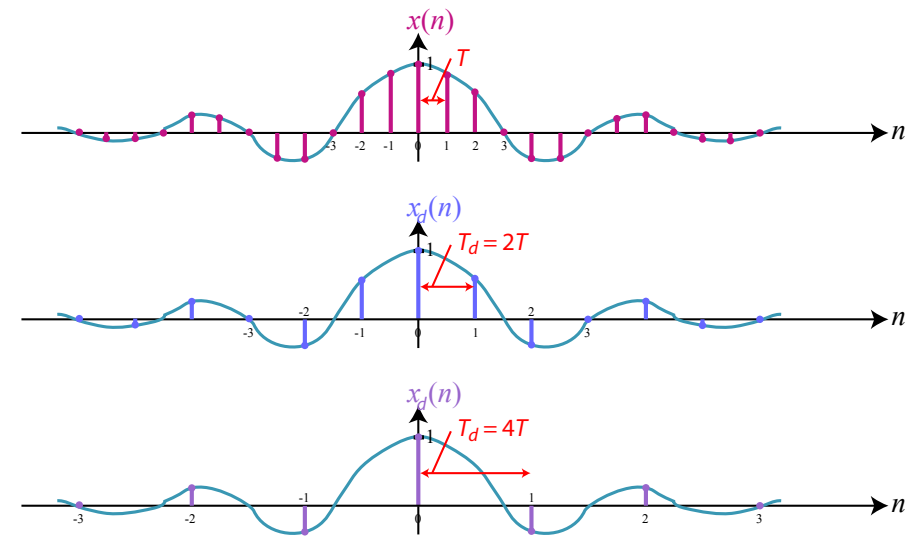
$$X(F) = \frac{1}{T} \sum_{k=-\infty}^{\infty} X_a\left(F - \frac{k}{T}\right)$$

$$X_d(F) = \frac{1}{DT} \sum_{k=-\infty}^{\infty} X_a\left(F - \frac{k}{DT}\right)$$

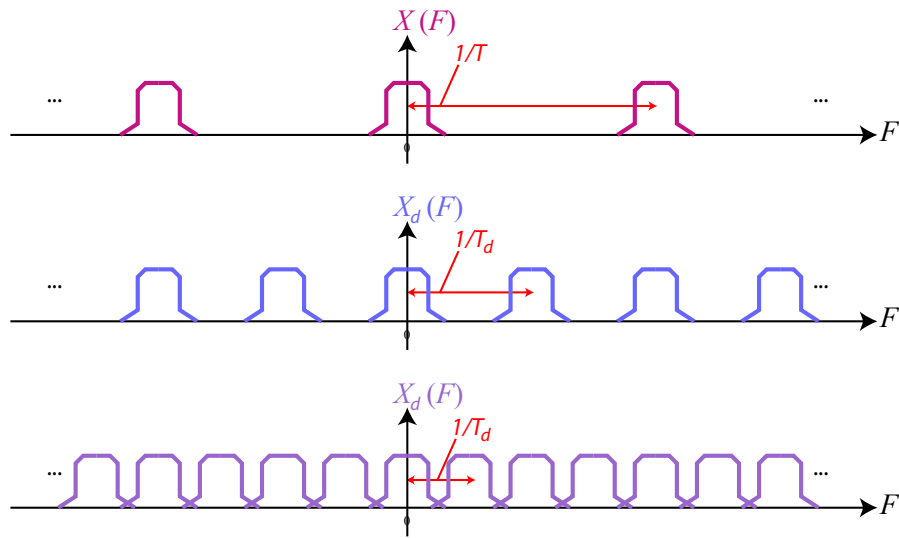
Decimation example: $D = 2$:



Decimation example: $D = 2, 4$:



Decimation example: $D = 2, 4$:



Sampling of Discrete-Time Signals

Therefore, from

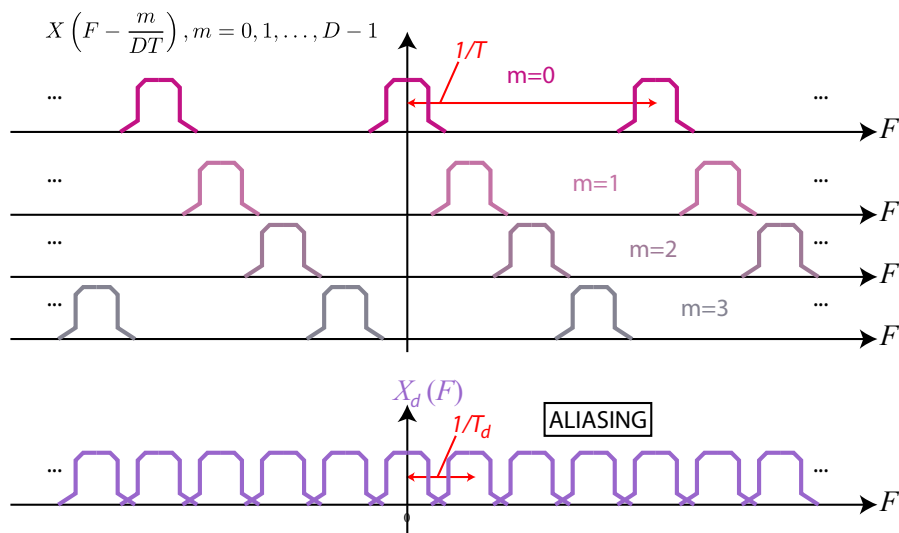
$$X(F) = \frac{1}{T} \sum_{k=-\infty}^{\infty} X_a \left(F - \frac{k}{T} \right)$$

$$X_d(F) = \frac{1}{DT} \sum_{k=-\infty}^{\infty} X_a \left(F - \frac{k}{DT} \right)$$

By inspection, we have:

$$X_d(F) = \frac{1}{D} \sum_{m=0}^{D-1} X \left(F - \frac{m}{DT} \right)$$

Decimation example: $D = 4$:



Aliasing from Decimation

Thus,

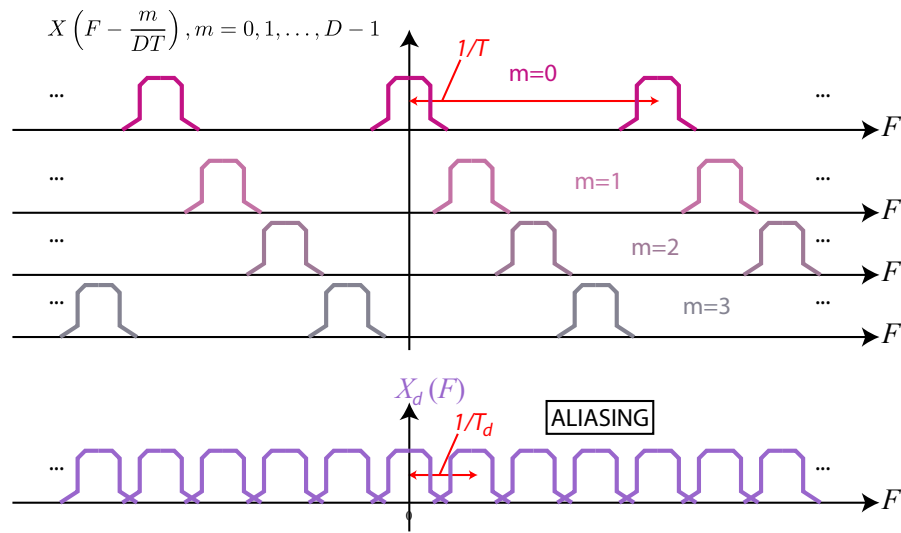
Cts-time Sampling $\iff X_a(F)$ repeated **infinite** times
 Dst-time Sampling $\iff X(F)$ repeated **finite** times

To avoid aliasing when decimating via factor D :

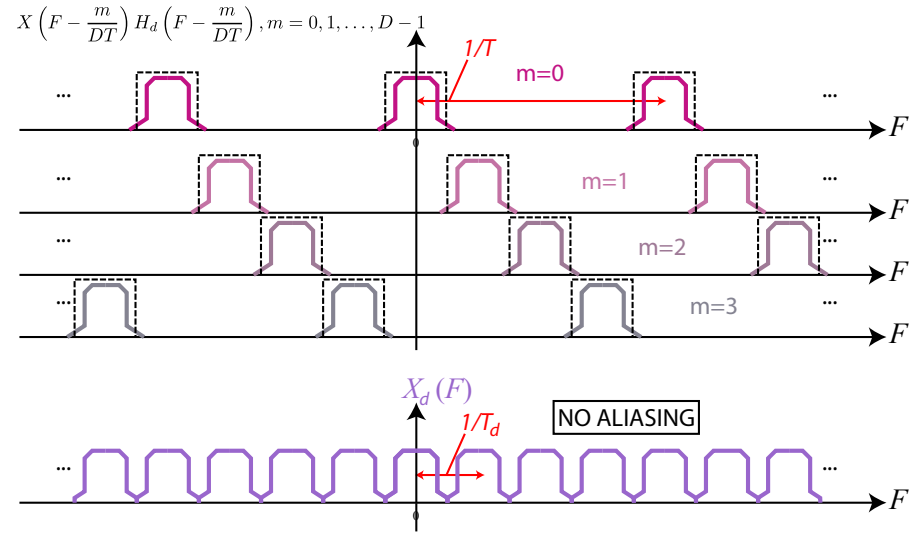
$$\text{Maximum Frequency} \leq \frac{1}{2DT}$$

Thus an **anti-aliasing** filter is applied prior to decimation.

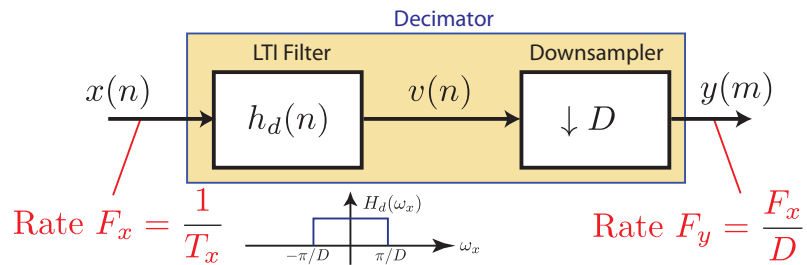
Decimation example: $D = 4$: no anti-aliasing filter



Decimation example: $D = 4$: anti-aliasing filter



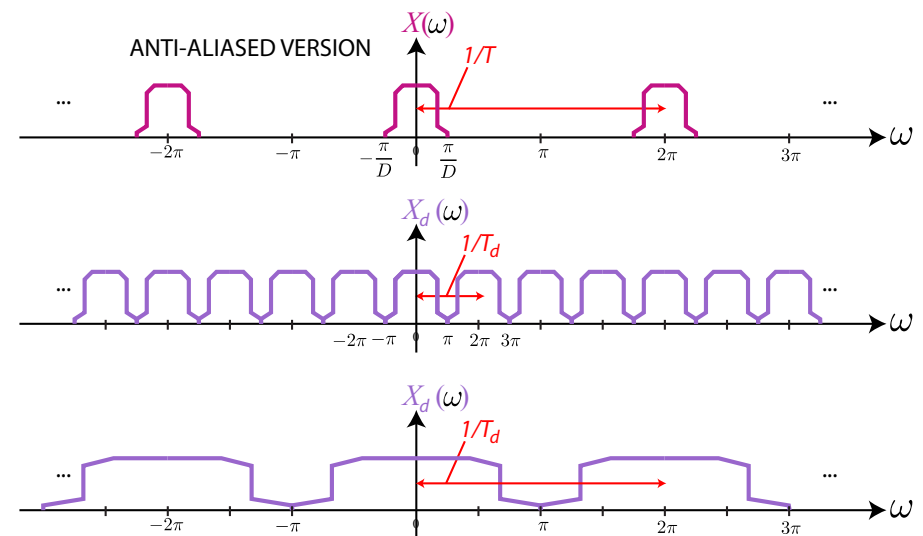
Downsampling with Anti-Aliasing Filter



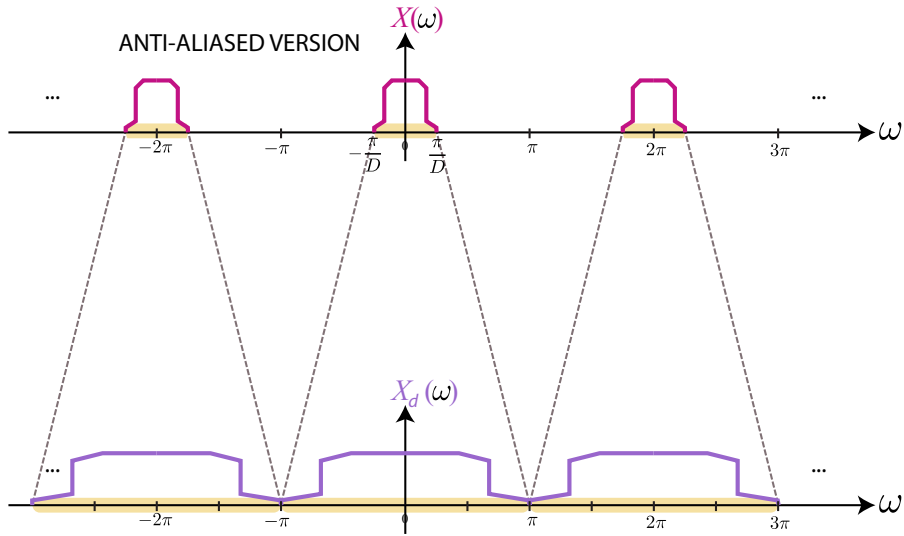
- The **anti-aliasing** filter $H_d(\omega)$ should have effective continuous-time frequency cutoff of $F_0 = \frac{1}{2DT}$ Hz, which is equivalent to a normalized cutoff of:

$$f_0 = \frac{F_0}{F_s} = \frac{1}{2DT} \cdot \frac{1}{F_s} = \frac{1}{2D} \quad \text{or} \quad \omega_0 = 2\pi \frac{1}{2D} = \frac{\pi}{D}$$

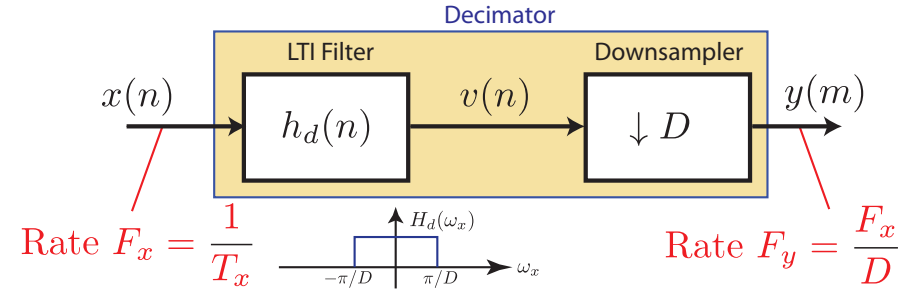
$$-\pi/D \leq \omega \leq \pi/D \text{ is expanded into } -\pi \leq \omega \leq \pi$$



$$-\pi/D \leq \omega \leq \pi/D \text{ is expanded into } -\pi \leq \omega \leq \pi$$

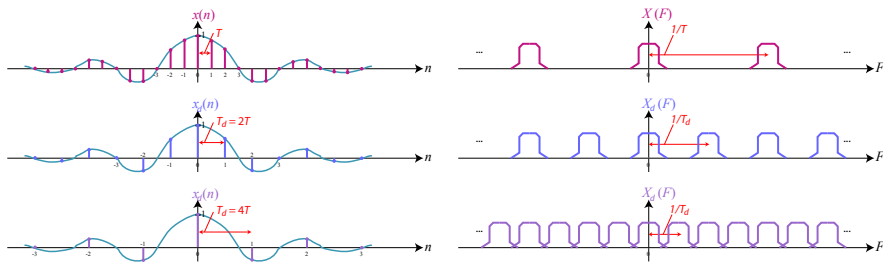


Interpolation by a Factor I



- ▶ Decimation keeps every D th point giving a higher rate of change to the signal.
- ▶ The decimation process stretches an anti-aliased signal such that it contains higher frequency components.
- ▶ Thus, decimation generally speeds up an audio signal, making it appear to have higher tonal characteristics.

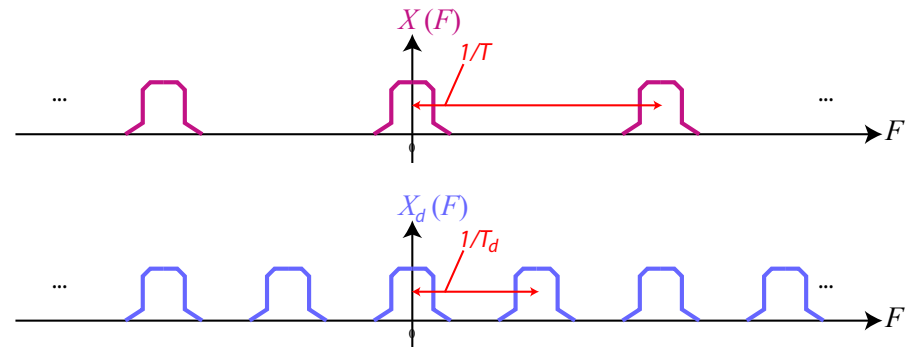
Interpolation of Discrete-time Signals



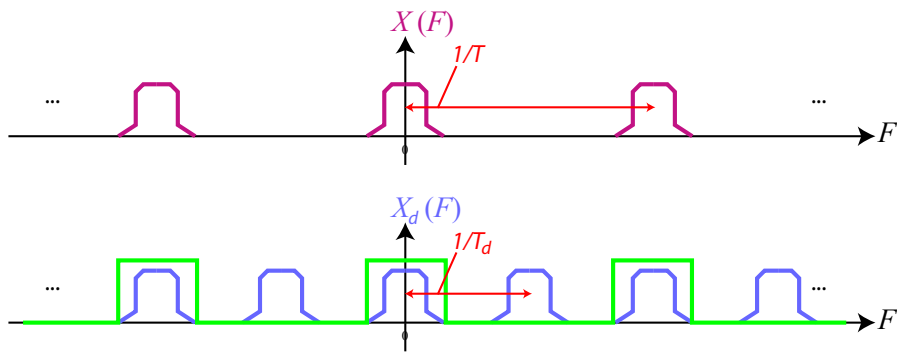
- ▶ Interpolation for $T_d = \frac{T}{D}$ is possible if no aliasing exists in the signal to be interpolated.

Note: We will later change D to I to distinguish between the decimation and interpolation factors. We use D here for simplicity as interpolation is being described, in part, as the *reverse process* of decimation.

Interpolation of Discrete-time Signals



Interpolation of Discrete-time Signals



Interpolation of Discrete-time Signals

Analysis Strategy:

- ▶ We consider the process of **discrete-time interpolation**; i.e., obtaining $x(n)$ from its decimated version $x_d(n) = x(nD)$.
- ▶ We will assume that **no aliasing** resulted from the decimation process.
- ▶ We will determine a relationship between $x(n)$ and $x_d(n)$ in the following way:
 1. Let us mathematically reconstruct $x_a(t)$ from $x_d(n)$ assuming a sampling period of DT .
 2. Let us then sample $x_a(t)$ with a sampling period of T to construct $x(n)$.

Interpolation of Discrete-time Signals

Step 1: $x_a(t)$ can be reconstructed from $x_d(n)$ as follows:

$$x_a(t) = \sum_{m=-\infty}^{\infty} x_d(m) \frac{\sin \frac{\pi}{DT}(t - mDT)}{\frac{\pi}{DT}(t - mDT)}$$

Step 2: Sample $x_a(t)$ to produce $x(n)$:

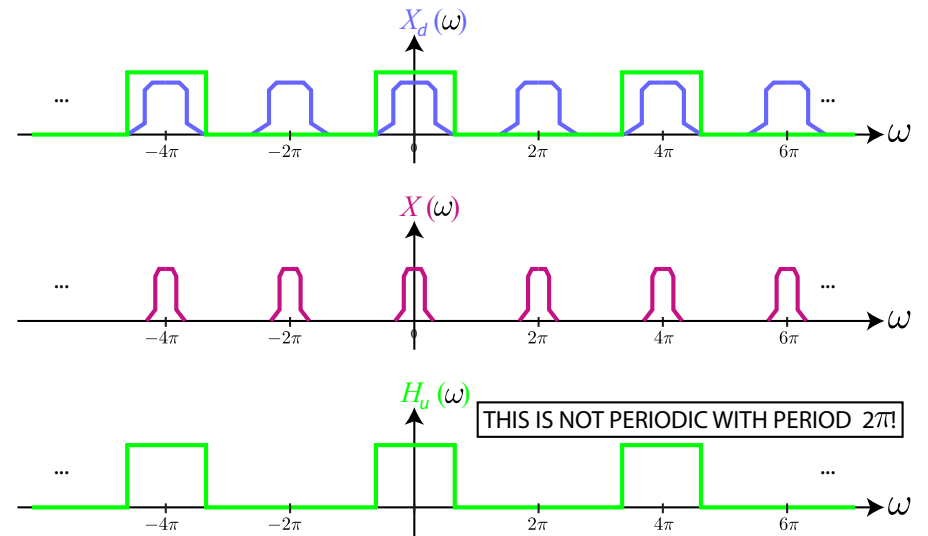
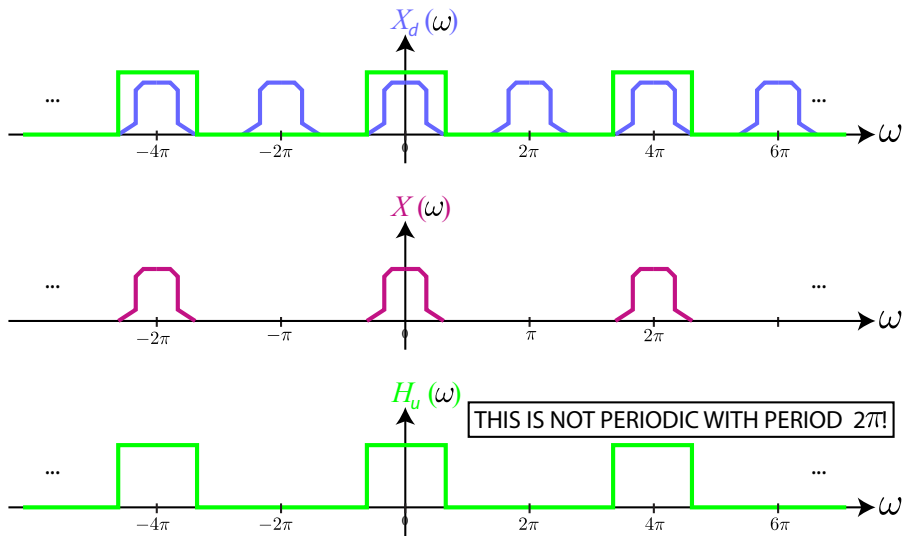
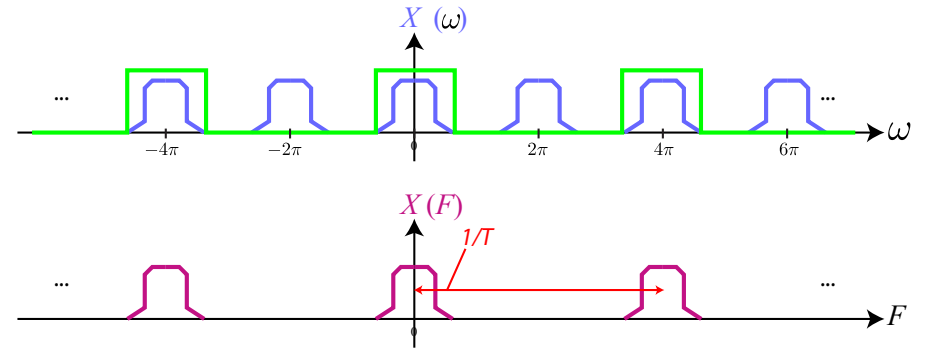
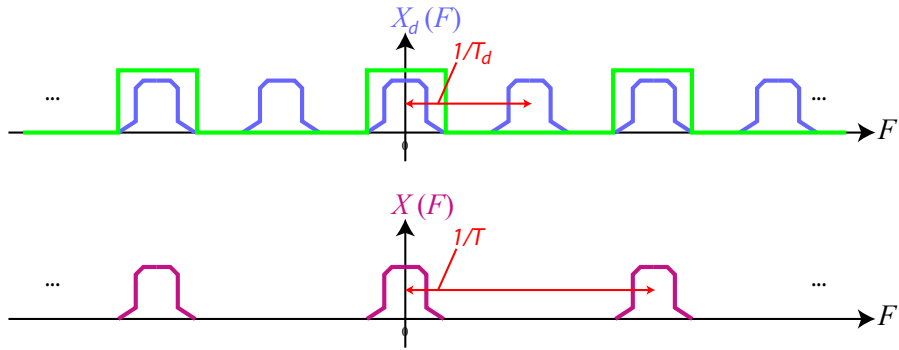
$$\begin{aligned} x(n) = x_a(nT) &= \sum_{m=-\infty}^{\infty} x_d(m) \frac{\sin \frac{\pi}{DT}(nT - mDT)}{\frac{\pi}{DT}(nT - mDT)} \\ &= \sum_{m=-\infty}^{\infty} x_d(m) \frac{\sin \frac{\pi}{D}(n - mD)}{\frac{\pi}{D}(n - mD)} \end{aligned}$$

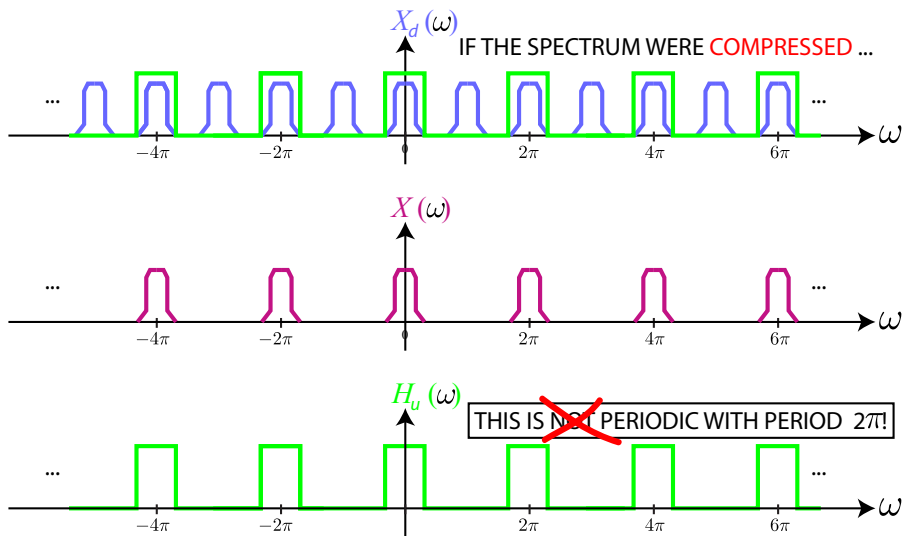
Interpolation of Discrete-time Signals

$$\begin{aligned} x(n) &= \sum_{m=-\infty}^{\infty} x_d(m) \left[\frac{\sin \frac{\pi}{D}(n - mD)}{\frac{\pi}{D}(n - mD)} \right] \\ &= \sum_{m=-\infty}^{\infty} x_d(m) g_{BL}(n - mD) \end{aligned}$$

where

$$g_{BL}(n) = D \frac{\sin(\pi/D)n}{\pi n} \xleftrightarrow{\mathcal{F}} G_{BL}(\omega) = \begin{cases} D & |\omega| \leq \frac{\pi}{D} \\ 0 & \frac{\pi}{D} < |\omega| \leq \pi \end{cases}$$



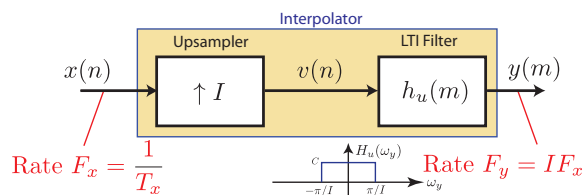


Interpolation of Discrete-time Signals

To achieve this, consider a two-stage process:

- ▶ Stage 1: **Upsample** to appropriately **compress** the spectrum.
 - ▶ Stage 2: Then filter with an appropriate lowpass filter.
-
- ▶ We will consider upsampling by a factor of I .
 - ▶ Note: we change here the interpolation factor from D to I to distinguish our results from decimation.

Interpolation of Discrete-time Signals

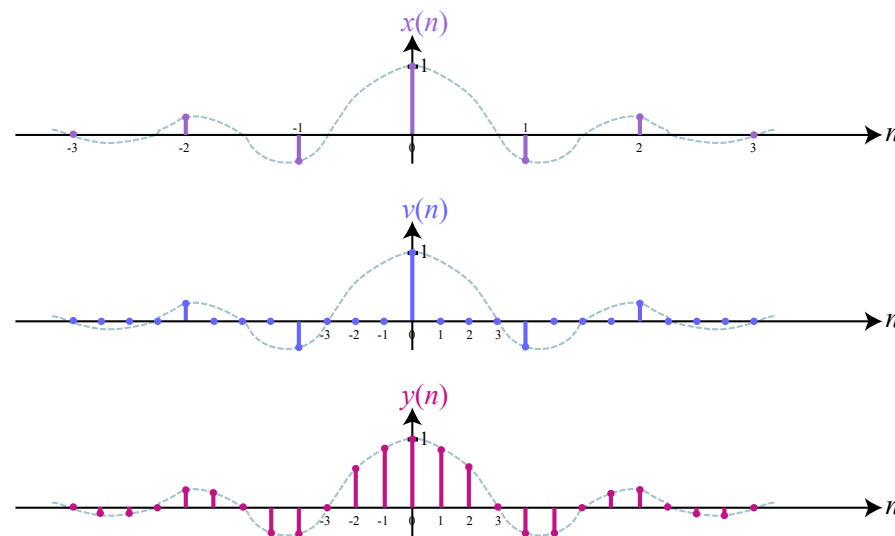


▶ Upsampling (without filtering) can be represented as:

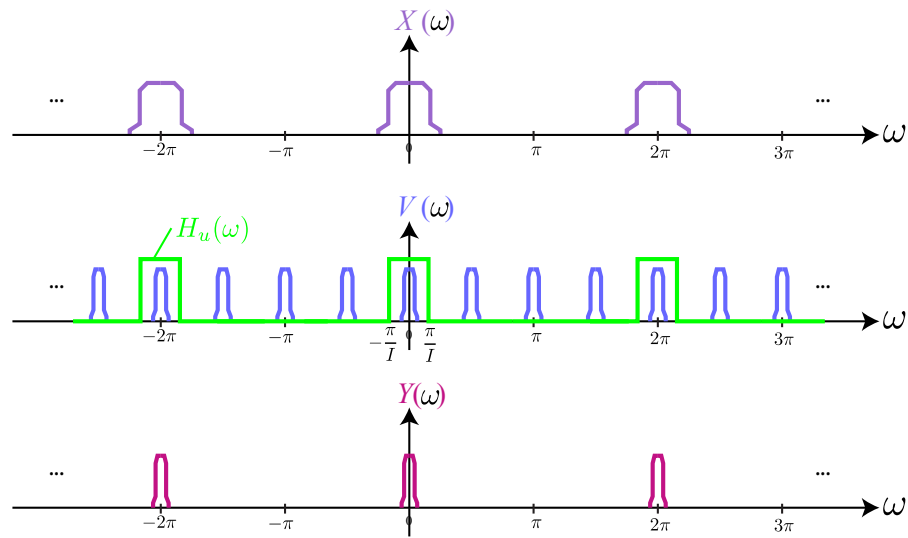
$$v(m) = \begin{cases} x(m/I) & m = 0, \pm I, \pm 2I, \dots \\ 0 & \text{otherwise} \end{cases}$$

$$V(\omega) = X(\omega I)$$

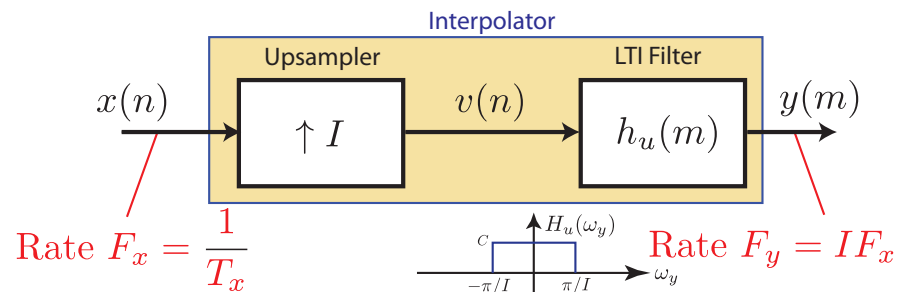
Interpolation example: $I = 4$: upsampling + lowpass filtering



Interpolation example: $I = 4$: upsampling + lowpass filtering



Interpolation by a Factor I



- ▶ Interpolation only increases the visible resolution of the signal. No new information is gained.
- ▶ Interpolation generally slows down an audio signal, making it appear to have lower tonal characteristics.

Overall,

$$V(\omega) = X(\omega I)$$

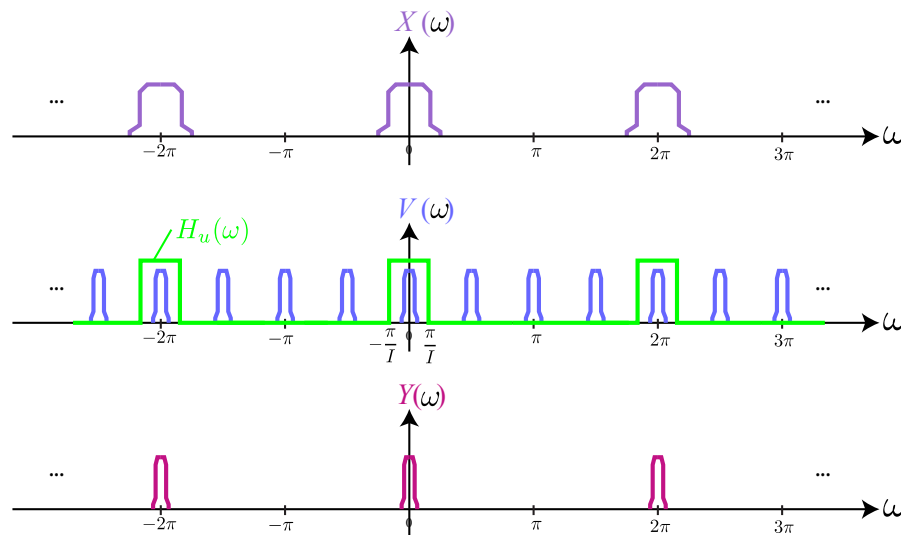
$$H_u(\omega) = \begin{cases} I & 0 \leq |\omega| \leq \pi/I \\ 0 & \text{otherwise} \end{cases}$$

$$Y(\omega) = H_u(\omega)V(\omega) = \begin{cases} IX(\omega I) & 0 \leq |\omega| \leq \pi/I \\ 0 & \text{otherwise} \end{cases}$$

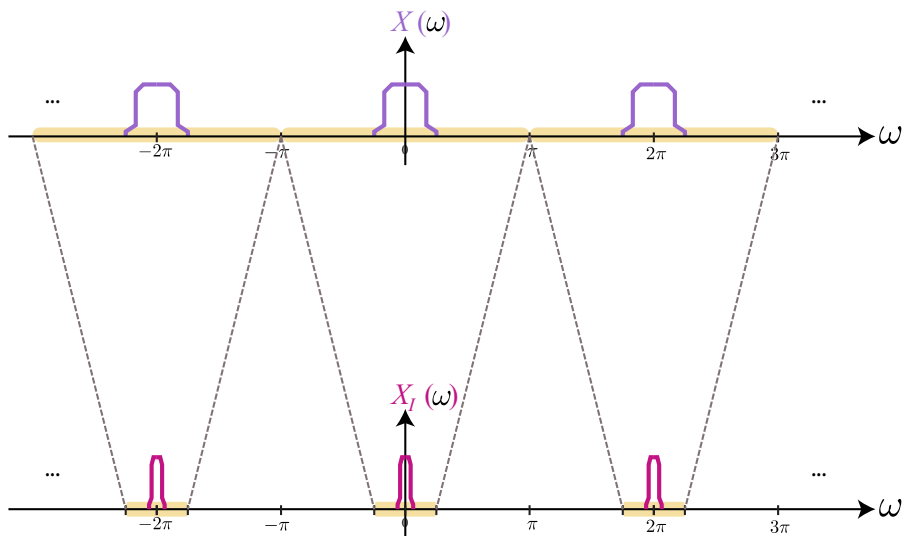
$$Y(\omega) = \begin{cases} IX(\omega I) & 0 \leq |\omega| \leq \pi/I \\ 0 & \text{otherwise} \end{cases}$$

$-\pi \leq \omega \leq \pi$ is compressed into $-\pi/I \leq \omega \leq \pi/I$

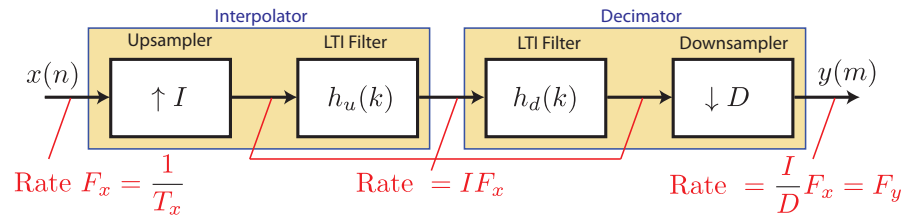
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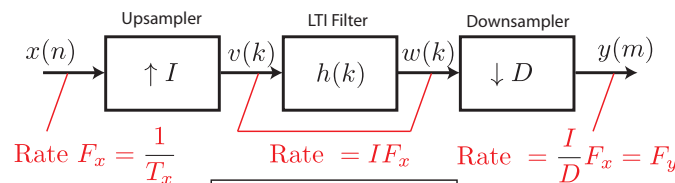
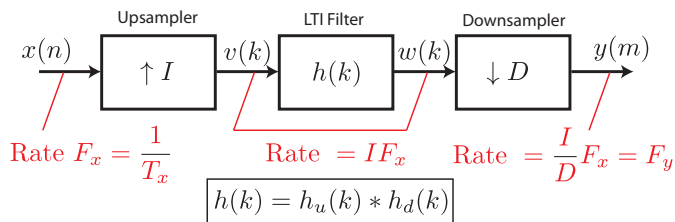
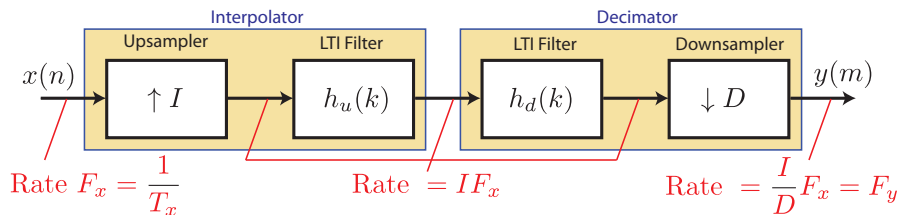


Sampling Rate Conversion by I/D

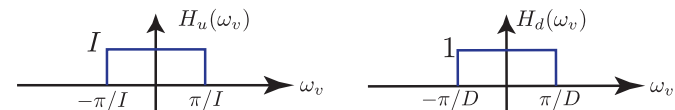


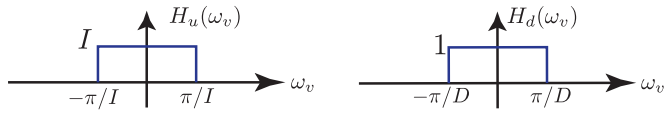
- ▶ $x(n)$: original samples at sampling rate F_x
- ▶ $y(n)$: new samples at sampling rate F_y

Sampling Rate Conversion by I/D



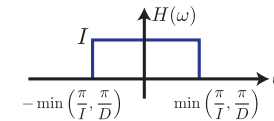
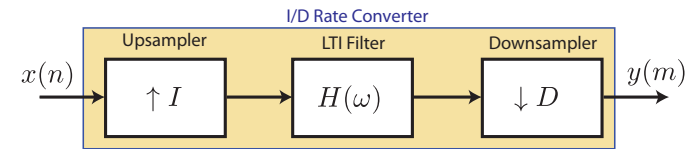
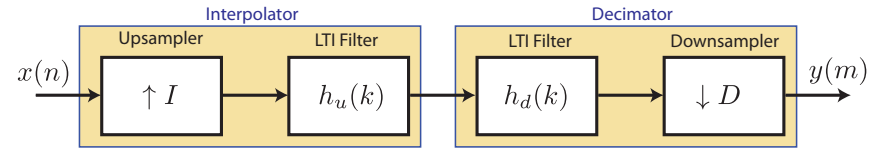
$$h(k) = h_u(k) * h_d(k)$$





$$H(\omega) = H_u(\omega)H_d(\omega) = \begin{cases} I & 0 \leq |\omega| \leq \min(\pi/D, \pi/I) \\ 0 & \text{otherwise} \end{cases}$$

Sampling Rate Conversion by I/D



- ▶ Thus, a wide variety of sound speed conversions is possible through a combination of upsampling, LTI filtering and downsampling.

