

Effect of Delay and Buffering on Jitter-Free Streaming over Random VBR Channels

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Abstract

We study the optimal streaming of variable bit-rate (VBR) video over a random VBR channel. The goal of a streaming application is to enable the successful decoding of each video object before its displaying deadline is violated. Hence, we define the main performance metric of a streaming system as the probability of un-interrupted video presentation, or jitter-free probability. Previous literature has described solutions to estimate the jitter-free probability by assuming either independence in the encoded data process or simplistic channel models. In this work, we present a novel analytical framework, which requires only the maximum channel bit rate and some statistical information of an arbitrary VBR channel, to bound the probability of jitter-free playback under the constraint of initial playback delay and receiver buffer size. Both the infinite and finite buffer cases are considered. This technique is then applied to investigate streaming over a wireless system modelled by an extended Gilbert channel with ARQ transmission control. Experimental results with MPEG-4 VBR encoded video demonstrates that the proposed analysis derives close bounds to the actual system performance. Finally, we show that the proposed analysis provides a theoretical foundation to quantify the tradeoffs between the initial playback delay, the receiver buffer size, and the jitter-free probability for a general class of VBR streaming over random VBR channels.

Index Terms

EDICS: 5-STRM; multimedia streaming, performance modeling, playback delay, receiver buffering, playback interruption

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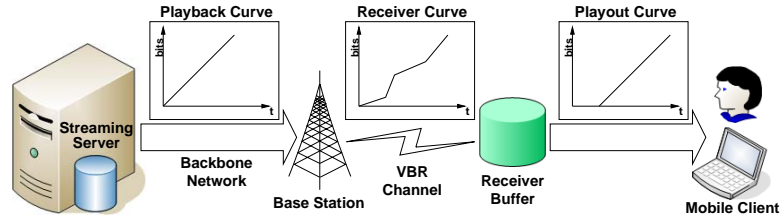


Fig. 1. A typical media streaming system.

I. INTRODUCTION

Mobile devices of the near future are expected to bring ubiquitous access to streaming multimedia services, such as TV news, music video, and online movies. Streaming multimedia are likely to become major applications in future mobile systems and may indeed be a key factor for their success. However, both wired and wireless, but especially wireless, multimedia delivery face several challenges, such as bandwidth scarcity, random channel variation, and limited storage capacity [1]. In this work, we focus on the streaming of pre-encoded video to mobile clients, taking into account these system constraints and limited resources.

A general media streaming system is shown in Figure 1. It consists of a media streaming *server*, a *transport channel*, and a streaming *client*. The server stores a number of pre-encoded video objects in the wired backbone network. We consider general variable bit-rate (VBR) encoded videos with non-linear playback curves [2]. These video objects are accessed by the clients, through a wire or wireless access network.

In general, the transmission rate of the channel varies over time. Video display interruption may occur if data are not delivered on time when the transmission rate does not match the encoded rate. The event of playback interruption is termed *jitter*. Clearly, jitter reduces the perceived video quality and is undesirable in video streaming.

To alleviate the detrimental effect of channel and data bit rate variation on jitter-free playback,

a common approach is to delay the initial playback of a stream through buffering at the receiver. The challenges are two-fold. First, both buffer underflow and buffer overflow may occur and lead to jittering. Hence, a suitable buffer size must be determined. Second, as we are interested in providing continuous video streaming service, the initial playback delay should be minimized.

In this work, we present an analytical framework to quantify the fundamental tradeoffs between the initial playback delay, the receiver buffer size, and the jitter-free playback probability, in order to optimize the streaming of VBR encoded video over a random VBR channel. Our main contributions are three-fold. *First*, we derive the upper and lower bounds of jitter-free probability given the initial playback delay and receiver buffer size, for both infinite buffers and finite buffers. The proposed analysis technique provides a means to maximize the jitter-free probability for a general class of VBR multimedia streaming over random VBR channels. *Second*, we apply the proposed analytical framework toward optimal streaming over a general wireless network. Numerical analysis results are obtained for wireless systems modelled by an extended Gilbert-Elliot channel with ARQ transmission control. *Third*, experiments using sample MPEG-4 video traces are carried out to validate the proposed analysis and provide new insights into the optimal balancing of the initial playback delay and the receiver buffer size for optimal multimedia streaming.

The rest of this paper is organized as follows. We discuss related works in Section II. In Section III, an analytical framework is presented to bound the jitter probability under constraints of initial delay and receiver buffer size. This framework is applied to a wireless system to derive QoS bounds in Section IV. Section V provides the numerical and experimental results and discusses the performance tradeoffs. Conclusions are drawn in Section VI.

II. RELATED WORK

One obvious way to avoid jitter is to start displaying the video only after it is fully downloaded. By doing this, jitter is 100% avoidable, but it also results in the longest initial delay and the maximal buffer size, which is generally unacceptable, especially for small wireless devices. In practice, the system buffers a certain portion of video data at the client before displaying the video, so that transient packet losses and delay do not constantly interrupt the playback of the stream. Intuitively, the more data is buffered, the lower is the probability of jitter, but the startup delay induced by buffering increases, too. For this reason, system designers must trade the reliability of uninterrupted playback against delay and buffer size.

In this context, Sen *et al* proposed an online smoothing technique for VBR streaming video in [3] by introducing a few seconds of startup delay and a client buffer to compensate for the variation of video encoding rate. The authors of [4] used network calculus analysis to derive an optimal multimedia smooth scheme. However, both schemes require a dedicated smoothing server or an intermediate smoothing node and only consider a wired network offering guaranteed bandwidth service. Therefore these schemes are not suitable for error-prone networks such as wireless streaming systems.

The authors of [5] introduced the concept of having two buffers at the receiver - a delay jitter buffer and a decoder buffer. The delay jitter buffer is used to compensate for the delay jitter introduced by the channel and to reduce bit rate variations caused by the VBR behavior of the channel. Streaming video data is first buffered in the delay jitter buffer and then is emitted into the decoder buffer at a constant rate R after a initial delay Δ_1 . By choosing a suitable Δ_1 , the jittered streaming data is de-jittered by the delay jitter buffer and a virtual CBR channel with rate R is formed at the input of the decoder buffer. Therefore, traditional hypothetical reference

decoders (HRD) such as the video buffer verifier (VBV) for MPEG-2 or the H.263 HRD can be applied.

In [6], the authors compared the single receiver buffer approach with the aforementioned separate buffer approach and showed that a single receiver buffer always performs at least as good as two separate buffers. They then described a method to provide a certain QoS guarantee, where the initial delay and receiver buffer size are decided according to the upper and lower bounds of the random receiver curve, $R(t)$, to guarantee a minimum jitter-free probability. However, they did not give a general means to find such bounds of $R(t)$, and only a simple Bernoulli channel was considered.

A Markov chain analysis method was introduced in [7] to examine the tradeoff between the buffer underflow probability and the latency for Adaptive Media Playout (AMP) video streaming. Applying the two-state Gilbert-Elliott lossy channel model [8], [9], this method represents the streaming system with a Markov chain whose states are described as a combination of the buffer state, the channel state and the playout position. Representing underflow event as an absorption state, this method gives the underflow probability by solving the Markov chain. However, in order to construct a Markov chain, the transmission times of the data frames are assumed to be independent and identically distributed (i.i.d.) random variables, which is may not be realistic for VBR encoded video streaming where the frame sizes are different. Other previous research studies on jitter reduction include works on rate-distortion optimized video streaming [10], [11], [12]. They require significant modifications in the streaming server, the streaming client, or both.

In this work, we consider the single receiver buffer setup as in [6] and propose a novel analytical framework to bound the jitter probability for generic VBR streaming video over random VBR channels. The proposed framework can be applied to most general systems and only

requires basic statistical information about the channel. To the best of our knowledge, this paper represents the first attempt to analytically quantify the tradeoffs between initial playback delay, receiver buffer size, and the jitter free probability for streaming with arbitrary encoding scheme and arbitrary random channels.

III. STREAMING VIDEO OVER VBR CHANNELS

In this section, we provide an analytical framework to bound the jitter-free probability for generic VBR streaming over random VBR channels. The application of this analysis to a case study on wireless network streaming is presented in the next section.

A. System Model

We consider the same video streaming system as in [6]. It consists of a video streaming server, a VBR transport channel, and a streaming client. Pre-encoded video objects are stored in the server. Each video object is characterized by a *playback curve* $p(t)$. The playback curve describes the total amount of data that have to be received by time t . It is generally assumed that $p(t) = 0$ for $t \leq 0$ and $p(t) = p(L)$ for $t \geq L$, where L is the length of the video in time and $p(L)$ is the size of the video in bits. The playback curve is assumed to be included in the preamble of the video stream and is available to the receiver [6].

When a client requests a video object, after setting up a connection, the server starts to stream video data to the client through the transport channel. The channel is assumed to be error free, possibly due to an ideal error control mechanism, such as coding or ARQ, but its bit rate may vary over time. This VBR channel is characterized by a random *receiver curve* $R(t)$, which specifies the total amount of data received error-free up to time t at the client side. We also assume $R(t) = 0$ for $t \leq 0$, which is reasonable since no data should be received before

the transmission begins. Clearly, both of $p(t)$ and $R(t)$ are monotonically increasing. This is a generalization of the CBR channel case in which the receiver curve is linear, i.e., $r(t) = Rt \cdot u(t)$.

As we are interested in providing continuous video streaming service, our objective is to minimize the initial playback (“startup”) delay Δ and the corresponding receiver buffer size B , while maintaining jitter-free playback, for a VBR channel. For jitter-free playback, both buffer underflow and overflow at the receiver buffer need to be eliminated. To avoid buffer underflow, the startup delay Δ has to be chosen such that for any time instant t , at least $p(t - \Delta)$ bits are available at the decoder, i.e.,

$$\{\Delta \in \mathfrak{R} : \forall t \leq L, R(t) \geq p(t - \Delta)\}. \quad (1)$$

Furthermore, to avoid buffer overflow, the buffer size B has to be large enough such that at any time instant t , all received non-decoded data can be stored in the receiver buffer, i.e.,

$$\{B \in \mathfrak{R} : \forall t \leq L, R(t) \leq p(t - \Delta) + B\}. \quad (2)$$

The right-hand side of (1) defines a *delayed playback curve*, and the right-hand side of (2) defines a *buffer limit curve*.

If a *deterministic* receiver curve $R(t)$ and the playback curve $p(t)$ are known before transmission at the streaming server, the authors of [6] have proven that the minimum startup delay to avoid buffer underflow should be chosen as

$$\Delta = \max_t \{t - p^{(-1)}(R(t))\}, \quad (3)$$

where $p^{(-1)}(x) \triangleq \min\{t : x \leq p(t)\}$ is the so called the pseudoinverse function of the monotonically increasing playback curve $p(t)$. And the corresponding minimum receiver buffer

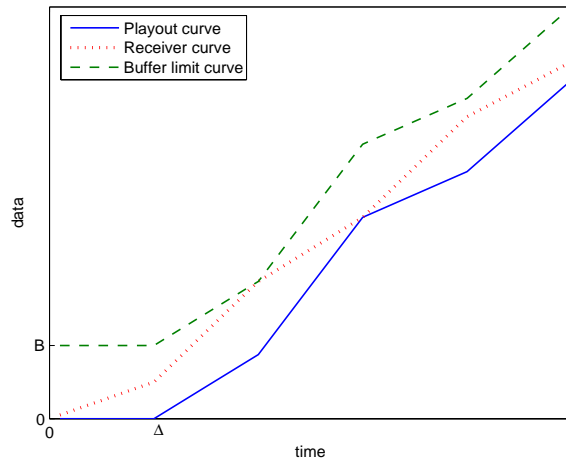


Fig. 2. Playback, receiver, and buffer-limit curves with their associated startup delay Δ and buffer size B .

size to avoid buffer overflow is then chosen as

$$B = \max_t \{R(t) - p(t - \Delta)\} \quad (4)$$

The optimal selection of Δ and B is illustrated in Figure 2.

However, in general, $R(t)$ is random and not known in advance, either at the transmitter or at the receiver. In this work, we focus on the problem of optimal streaming over VBR channels with a random $R(t)$, described in detail next in Section III-B.

B. Random Receiver Curve

The assumption that $R(t)$ is known in advance at the transmitter or receiver is obviously not realistic for most practical systems. To the best of our knowledge, there is no known method to specify the minimum startup delay without exact knowledge of the receiver curve. However, in general, users may still be satisfied if the playback jitters do not occur too frequently. Therefore, it is reasonable to guarantee a certain performance criterion, by specifying the probability that

the transmission of a video is successful without any buffer underflow or buffer overflow, given the constraint of startup delay and receiver buffer size.

To formalize the problem, let us consider a stationary-increment random process $R(t)$ that describes the random receiver curve introduced by the random channel. Obviously, each realization of the random process has the same monotonic properties as the deterministic receiver curve as we defined before. We want to determine the *jitter-free probability*, denoted by π , that a realization of $R(t)$ is entirely within the region between the delayed playback curve, $p(t - \Delta)$, and the buffer limit curve, $p(t - \Delta) + B$, during the playback period of a video, i.e.,

$$\pi \triangleq \Pr \{ \forall t \leq L, p(t - \Delta) \leq R(t) \leq p(t - \Delta) + B \}. \quad (5)$$

Generally, π is a difficult quantity to compute exactly, even if we know the stochastic properties of $R(t)$. Next, we will derive a lower bound and an upper bound of π , given some statistical information of $R(t)$.

C. Infinite Receiver Buffer Case

Let us first look at the case with infinite receiver buffer, i.e., $B = \infty$ or B is sufficiently large for any practical purposes such that the buffer never overflows. Assume we know that the bit rate of the VBR channel is upper bounded by b_{max} , i.e., $R'(t) \leq b_{max}$. In the best case, the VBR channel stays at the maximum bit rate b_{max} throughout the transmission. Without loss of generality, we fix the origin at the time instant when the client starts playing out the video. Then the receiver curve in the best case is

$$R_{min}(t) = b_{max}(t + \Delta_{min}) \cdot u(t + \Delta_{min}) \quad (6)$$

where $u(t)$ is the unit step function

$$u(t) = \begin{cases} 0, & t < 0 \\ 1, & t \geq 0 \end{cases}, \quad (7)$$

and Δ_{min} is the minimal achievable startup delay given by (3) with $R(t) = b_{max}t \cdot u(t)$, i.e.,

$$\Delta_{min} = \max_t \{t - p^{-1}(b_{max}t \cdot u(t))\}. \quad (8)$$

Note that Δ_{min} can only be achieved in the best case. It is in fact the minimum *supportable* startup delay. By supportable, we mean

$$\Pr \{\forall t \leq L, R(t) \geq p(t) \mid \forall t \leq -\Delta, R(t) = 0\} > 0. \quad (9)$$

Therefore, the startup delay should be chosen such that $\Delta \geq \Delta_{min}$. The derivation of π then proceeds in two cases as shown in Figure 3.

Case I. $R_{min}(L) = p(L)$

Let $t_0 = \inf\{t : R(t) < R_{min}(t)\}$. If $t_0 < L$, it is easy to see that $R(t) < R_{min}(t)$, $\forall t \geq t_0$, as shown in Figure 3(a). And therefore at the end of the video, we will have

$$R(L) < R_{min}(L) = p(L). \quad (10)$$

According to the monotonically increasing property of $p(t)$, jitter is inevitable for this $R(t)$. Then, it is easy to show that, given a supportable startup delay Δ , the probability of continuous playback is

$$\pi = \Pr\{\forall t \leq L, R(t) \geq p(t)\}$$

$$\begin{aligned}
&= \Pr\{t_0 \geq L\} \\
&= \Pr\{\forall t \leq L, R(t) \geq R_{min}(t)\} \\
&= \Pr\{R(L) \geq R_{min}(L)\}.
\end{aligned} \tag{11}$$

Case II. $R_{min}(L) > p(L)$

We define the *latest most critical point* t_c of underflowing as

$$t_c = \max\{t : R_{min}(t) = p(t)\}, \tag{12}$$

and the *transmission finishing point* t_f in the ideal case with minimal startup delay Δ_{min} as

$$t_f = \frac{p(L)}{b_{max}} - \Delta_{min}. \tag{13}$$

Clearly, if $t_0 \geq t_f$, jitter does not occur; if $t_c \leq t_0 < t_f$, jitter may not occur with positive probability; and if $t_0 < t_c$, jitter occurs. An example when $t_0 < t_c$ is shown in Figure 3(b).

Hence we can derive a lower bound on π as follows:

$$\begin{aligned}
\pi &= \Pr\{t_0 \geq t_f\} + \Pr\{\forall t \leq L, R(t) \geq p(t) \text{ and } t_c \leq t_0 < t_f\} \\
&\geq \Pr\{t_0 \geq t_f\} \\
&= \Pr\{\forall t \leq t_f, R(t) \geq R_{min}(t)\} \\
&= \Pr\{R(t_f) \geq p(L)\} \stackrel{\Delta}{=} \pi_l.
\end{aligned} \tag{14}$$

Moreover, noticing that $\frac{d}{dt}p(t) < b_{max}$ for some $t \in [t_c, L]$, it is possible that even if a jitter incident occurs, $R(t)$ may increase faster than $p(t)$ and, at the end of the video, achieve $R(L) \geq p(L)$. Hence π is upper bounded by the probability of receiving no less than $p(L)$ bits

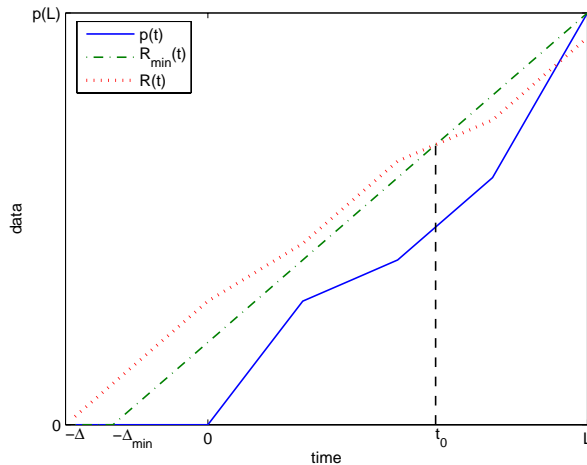
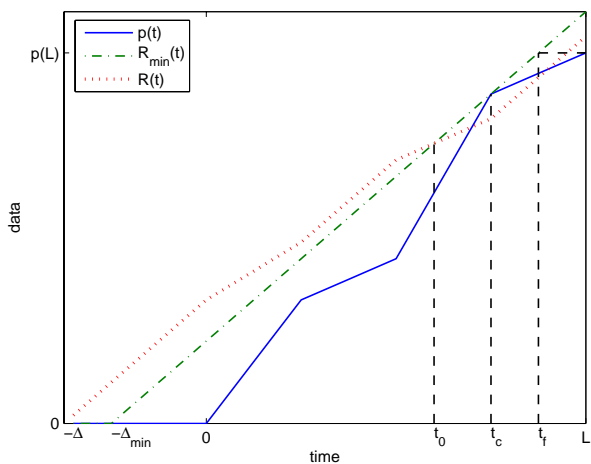
(a) Case I: $R_{min}(L) = p(L)$ (b) Case II: $R_{min}(L) > p(L)$, $t_0 < t_c$

Fig. 3. Examples of infinity receiver buffer.

by the end of the video, i.e.,

$$\pi \leq \pi_u \triangleq \Pr\{R(L) \geq p(L)\}. \quad (15)$$

In summary, when a supportable startup delay $\Delta \geq \Delta_{min}$ is chosen, the jitter free probability of a given playback curve $p(t)$ is bounded by π_l and π_u according to (14) and (15), respectively.

Both bounds are achieved iff $R_{min}(L) = p(L)$.

D. Finite Receiver Buffer Case

When the receiver buffer is not large enough, overflow may occur. We will derive bounds on the probability that neither underflow nor overflow occurs.

Let t_B denote the *first most critical* point of overflowing:

$$t_B = \min\{\arg \max_t \{R_{min}(t) - p(t)\}\}. \quad (16)$$

Obviously, if the buffer size is a design parameter, then B should be chosen such that

$$B \geq R_{min}(t_B) - p(t_B) \triangleq B_{min}. \quad (17)$$

Otherwise jitter (either overflow or underflow) is inevitable. Let

$$R_B(t) = b_{max}(t + \Delta_B), \quad (18)$$

where

$$\Delta_B = \min_t \left\{ \frac{p(t) + B}{b_{max}} - t \right\}, \quad (19)$$

is the *highest* supporting line of the buffer limit curve $p(t) + B$ with slope b_{max} . An example of this finite buffer case is shown in Figure 4.

We first consider a lower bound of π . It can be shown that

$$\begin{aligned} \pi &= \Pr\{\text{no underflow and no overflow}\} \\ &= \Pr\{\forall t \leq L, p(t) \leq R(t) \leq p(t) + B\} \\ &= \Pr\{\forall t \leq L, R(t) \geq p(t)\} \\ &\quad - \Pr\{\exists t \leq L, R(t) > p(t) + B \text{ and } \forall t \leq L, R(t) \geq p(t)\} \end{aligned}$$

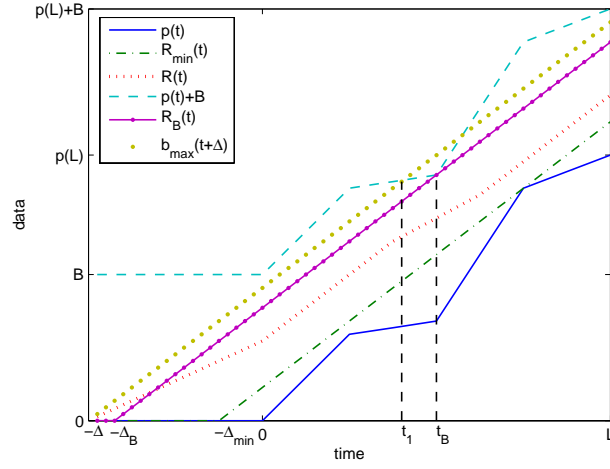


Fig. 4. An example of finite receiver buffer.

$$\begin{aligned}
&\geq \Pr\{\forall t \leq L, R(t) \geq p(t)\} - \Pr\{\exists t \leq L, R(t) > p(t) + B\} \\
&\geq \Pr\{R(t_f) \geq p(L)\} - \Pr\{\exists t \leq L, R(t) > p(t) + B\}.
\end{aligned} \tag{20}$$

Then, let

$$t_1 = \min\{t : b_{max}(t + \Delta) = p(t) + B\} \tag{21}$$

be the *first possible* point of overflowing when startup delay is Δ . It is easy to see that if $R(t_1) \leq R_B(t_1)$, overflow does not happen, i.e.

$$\Pr\{R(t_1) \leq R_B(t_1)\} \leq \Pr\{\forall t \leq L, R(t) \leq p(t) + B\}. \tag{22}$$

Hence, we have

$$\Pr\{R(t_1) > R_B(t_1)\} \geq \Pr\{\exists t \leq L, R(t) > p(t) + B\}. \tag{23}$$

Then from (20), we conclude that

$$\pi \geq \Pr\{R(t_f) \geq p(L)\} - \Pr\{R(t_1) > R_B(t_1)\}. \quad (24)$$

Following the same logic, if $R(0) \leq R_B(0)$, there will be no overflow, then we can also have

$$\pi \geq \Pr\{R(t_f) \geq p(L)\} - \Pr\{R(0) > R_B(0)\}. \quad (25)$$

So π can be lower bounded by

$$\pi \geq \Pr\{R(t_f) \geq p(L)\} - \min\{\Pr\{R(t_1) > R_B(t_1)\}, \Pr\{R(0) > R_B(0)\}\}. \quad (26)$$

Notice that when $t_1 > 0$, $R(t_1) > R_B(t_1)$ implies $R(0) > R_B(0)$, i.e.,

$$\Pr\{R(t_1) > R_B(t_1)\} \leq \Pr\{R(0) > R_B(0)\}. \quad (27)$$

The inverse is also true when $t_1 < 0$. Then (26) can be rewritten as

$$\pi \geq \Pr\{R(t_f) \geq p(L)\} - \Pr\{R(t_1^+) > R_B(t_1^+)\} \triangleq \pi_l. \quad (28)$$

Here $(\cdot)^+$ denotes $\max\{0, \cdot\}$, and we have used π_l to denote the lower bound for the jitter-free probability π .

To derive the upper bound, we note that if $R(t_B) > R_B(t_B)$, overflow occurs. Hence we have

$$\Pr\{\exists t \leq L, R(t) > p(t) + B\} \geq \Pr\{R(t_B) > R_B(t_B)\}. \quad (29)$$

Then π is upper bounded by:

$$\begin{aligned}
\pi &= \Pr\{\forall t \leq L, p(t) \leq R(t) \leq p(t) + B\} \\
&= \Pr\{\forall t \leq L, R(t) \geq p(t)\} \\
&\quad - \Pr\{\forall t \leq L, R(t) \geq p(t) \text{ and } \exists t \leq L, R(t) > p(t) + B\} \\
&= \Pr\{\forall t \leq L, R(t) \geq p(t)\} \\
&\quad \cdot (1 - \Pr\{\exists t \leq L, R(t) > p(t) + B \mid \forall t \leq L, R(t) \geq p(t)\}) \\
&\leq \Pr\{\forall t \leq L, R(t) \geq p(t)\} \\
&\quad \cdot (1 - \Pr\{\exists t \leq L, R(t) > p(t) + B\}) \\
&\leq \Pr\{R(L) \geq p(L)\} \cdot (1 - \Pr\{R(t_B) > R_B(t_B)\}) \\
&\triangleq \pi_u
\end{aligned} \tag{30}$$

The first inequality in (30) is due to the fact that the conditional probability of overflow given no underflow occurs is greater than the marginal probability of overflow, and the second inequality is due to a relaxation of t from the range $(0, L]$ to L . Here we use π_u to denote the upper bound for the jitter-free probability π .

IV. CASE STUDY: WIRELESS VIDEO STREAMING

In a wireless access network, because of the hostile radio channel condition resulting from multipath propagation, fading and scattering, packet delay and losses are common. In this section, we present a case study on how to apply the theoretical framework in Section III to evaluate the jitter-free probability of streaming in a generic wireless system with an ARQ transmission protocol.

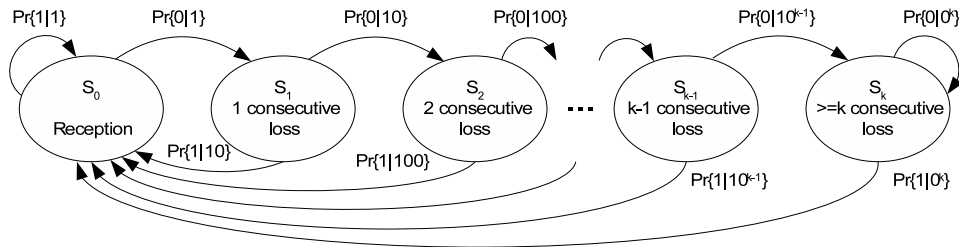


Fig. 5. A k -th order loss run-length (LRL) extended Gilbert model.

A. Modelling Wireless Channels

To properly model the error events in a wireless communication channel, we adopt in this work an extended Gilbert model proposed by Sanneck *et al.* in [13]. It is an generalization of the Gilbert-Elliott model [8], [9], one of the most widely adopted wireless channel representation in the literature. The Gilbert-Elliott model is a two-state Markov model where the channel switches between a “good state” (reception) and a “bad state” (loss). The channel state changes at the beginning of each time slot according to the given transition probabilities. A transmission is successful only if the channel is in the “good state”; otherwise, it fails. The Gilbert-Elliott model captures the temporal dependence in packet-loss processes for communication networks. However, many recent studies have shown that the Gilbert-Elliott model fails to predict performance measures depending on longer-term correlation of errors and hence can lead to lower channel capacity estimates and conservative allocation strategies [14], [15], [16], [17].

There are two categories of extended Gilbert models: those which describe reception run-lengths (RRL) and those which describe loss run-lengths (LRL). In what follows we concentrate on LRL models. As illustrated in Figure 5, for a k -th order LRL extended Gilbert model, there are $k + 1$ states, $\{S_0, S_1, \dots, S_k\}$. For each state, the subscript i represents the current loss run-length, except for state S_k , which represents the case that the current loss run-length is at least

k , in which case the system remains in state S_k with a subsequent loss or returns to S_0 with the first occurrence of reception. In each state, a reception event will bring the system back to state S_0 , the “good” state, which means the occurrence of a successful transmission will free the process from dependence upon past history and starts it anew. Hence, letting 0^i represent the occurrence of i successive losses, the LRL extended Gilbert model can be characterized in terms of the following $k + 1$ independent parameters:

- $\Pr\{1|10^i\}$: the probability that the next transmission succeeds, given that the current $LRL = i$, $0 \leq i \leq k - 1$;
- $\Pr\{1|0^k\}$: the probability that the next transmission succeeds, given that the current $LRL \geq k$;
- $\Pr\{0|10^i\} = 1 - \Pr\{1|10^i\}$; and
- $\Pr\{0|0^k\} = 1 - \Pr\{1|0^k\}$.

In addition, we model transmission control with a simple ARQ transmission protocol.¹ We consider a lossless system in which packets may be corrupted but acknowledgements are error free. After sending out a packet, the server waits until an ACK or an NACK arrives from the client. If an ACK is received, then the packet is correctly received and the server starts transmitting the next packet; if an NACK is received, or if a timeout interval is exceeded, the packet is considered corrupted and the server sends out the same packet again until an ACK is finally received. For simplified numerical analysis, we consider the system to be time-discrete and data are packed into packets of a fixed size. Each time slot is the time between when the server sends out a packet and when the corresponding acknowledgement arrives.

¹TCP is well known to misbehave in the wireless environment. In this work, we use simple ARQ to illustrate the behavior of a general error recovery protocol.

B. Delay and Buffer Design

We next derive the probability bounds π_l and π_u for the extended Gilbert model. Instead of looking into the probability $\Pr\{R[L] \geq N\}$ directly, let us first consider the random variable X_i , which represents the total number of transmissions that it takes to successfully transmit the i^{th} packet. Notice that except the first packet, every packet starts its transmission following a successful transmission of the previous packet. Hence, if a connection between the server and a client is setup with a successful transmission, then the channel is in the good state at $t = 0$ and $X = \{X_i\}$ is a sequence of i.i.d. random variables. Note that this only simplifies the presentation and does not significantly affect the results.

We denote $P_i = \Pr\{0|10^i\}$, $i = 0, 1, \dots, k-1$ and $P_k = \Pr\{0|0^k\}$. According to the extended Gilbert model above, we calculate the probability mass function of X

$$P_X[x] = \begin{cases} 1 - P_0, & x = 1 \\ (1 - P_{x-1}) \prod_{i=0}^{x-2} P_i, & x = 2, \dots, k \\ (1 - P_k) P_k^{x-(k+1)} \prod_{i=0}^{k-1} P_i, & x > k \end{cases} \quad (31)$$

and the moment generating function

$$\begin{aligned} \Phi_X(z) &\triangleq \sum_{k=1}^{\infty} P_X[k] z^{-k} \\ &= (1 - P_0) z^{-1} + \sum_{x=2}^k \left[(1 - P_{x-1}) z^{-x} \prod_{i=0}^{x-2} P_i \right] \\ &\quad + (1 - P_k) \prod_{i=0}^{k-1} P_i \sum_{x=k+1}^{\infty} P_k^{x-(k+1)} z^{-x} \end{aligned} \quad (32)$$

$$\begin{aligned}
&= (1 - P_0)z^{-1} + \sum_{x=2}^k \left[(1 - P_{x-1})z^{-x} \prod_{i=0}^{x-2} P_i \right] \\
&\quad + (1 - P_k) \prod_{i=0}^{k-1} P_i \frac{z^{-(k+1)}}{1 - P_k z^{-1}}, \quad |z| > P_k
\end{aligned} \tag{33}$$

Let $Y_N = \sum_{i=1}^N X_i$ be the total number of transmissions until the N^{th} packet is successfully transmitted. Then the moment generating function of Y_N is

$$\Phi_{Y_N}(z) = \Phi_X^N(z). \tag{34}$$

And the distribution function of Y_N is

$$\begin{aligned}
F_{Y_N}[y] &= \Pr\{Y_N \leq y\} \\
&= \sum_k P_{Y_N}[k] u[y - k] = P_{Y_N}[y] * u[y].
\end{aligned} \tag{35}$$

Here $u[n] = 1(n \geq 0)$ is the discrete unit step function and its z -transform is $(1 - z^{-1})^{-1}$, $|z| > 1$.

According to the convolution property of z -transform, we have

$$\begin{aligned}
\mathcal{Z}\{F_{Y_N}[y]\} &= \mathcal{Z}\{P_{Y_N}[y] * u[y]\} \\
&= \Phi_{Y_N}(z) \frac{1}{1 - z^{-1}} = \frac{\Phi_X^N(z)}{1 - z^{-1}}, \quad |z| > 1.
\end{aligned} \tag{36}$$

Obviously, the probability that the client has received at least N packets by time L equals to the probability that the transmission of the N^{th} packet is completed no later than $L + \Delta$, i.e., when $L + \Delta \geq N$, we have

$$\begin{aligned}
\Pr\{R(L) \geq N\} &= \Pr\{Y_N \leq L + \Delta\} = F_{Y_N}[L + \Delta] \\
&= \mathcal{Z}^{-1} \left\{ \frac{\Phi_X^N(z)}{1 - z^{-1}}, \quad |z| > 1 \right\}
\end{aligned}$$

$$\begin{aligned}
&= \frac{1}{2\pi j} \oint_C \frac{\Phi_X^N(z)}{1-z^{-1}} z^{L+\Delta-1} dz \\
&= \sum_{\xi \in \sigma} \operatorname{Res}_{z=\xi} \left[\frac{\Phi_X^N(z)}{1-z^{-1}} z^{L+\Delta-1} \right], \tag{37}
\end{aligned}$$

where C is a counterclockwise closed path encircling the unit circle, σ denotes the set of poles of $\Phi_X^N(z)z^{L+\Delta-1}/(1-z^{-1})$ within C , and $\operatorname{Res}_{z=\xi}$ denotes the residue at pole $z = \xi$. Then the lower bound π_l and upper bound π_u can be obtained by plugging (37) into (14), (15), (28) and (30). These analytical results are validated by experimenting with VBR video traces shown in the next section.

V. EXPERIMENTAL AND NUMERICAL RESULTS

In this section, we present experimental results to validate the proposed analytical framework. We investigate the effects of the initial playback delay and the receiver buffer size on jitter-free streaming and discuss the optimal balance between playback delay and buffer size.

A. Experimental Setup

We experiment on wireless streaming using MPEG-4 VBR video traces provided by [18]. Figure 6 shows the playback curves $R(t)$ for the first 40 seconds of three video sequences and their corresponding $R_{min}(t)$ values. Some main statistics of these video clips, pertinent to the computation of jitter-free probability bounds, are listed in Table I. These sequences were encoded at a constant frame rate of 25 frames per second in the Quarter Common Intermediate Format (QCIF) resolution (176×144). We have chosen the QCIF format because we are particularly interested in wireless networking systems where hand-held wireless devices typically have a screen size that corresponds to the QCIF video format.

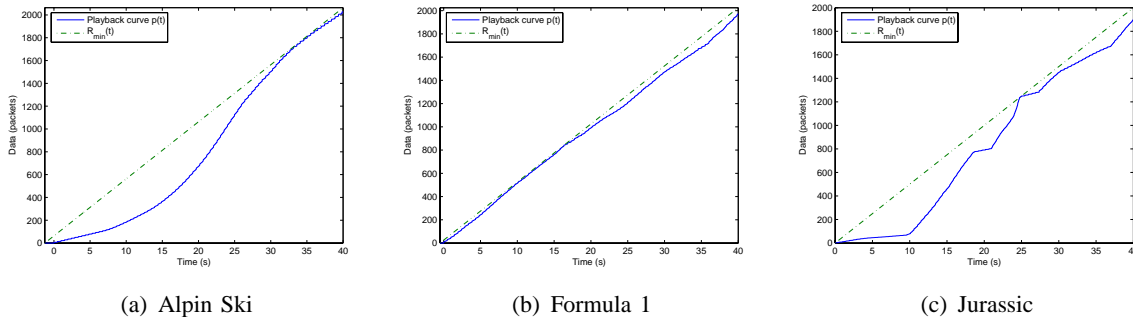


Fig. 6. VBR video playback curves and the corresponding $R_{min}(t)$.

Video name	Parameters of the video stream				
	Mean bit rate (per sec)	Peak bit rate (per sec)	Δ_{min} (s)	B_{min} (bits)	t_B (s)
Alpin Ski	1.8247e+05	3.0248e+06	1.26	1.638e+06	15.36
Formula 1	1.7754e+05	2.1428e+06	0.5	3.826e+05	36
Jurassic	1.7100e+05	3.1668e+06	0	1.530e+06	10.08

TABLE I
PARAMETERS OF DIFFERENT VIDEO STREAMS

For numerical analysis, we adopt a three-state extended Gilbert model (e.g., $k = 2$), with state transition probabilities $\Pr\{0|1\} = 0.005$, $\Pr\{0|10\} = 0.9$ and $\Pr\{0|00\} = 0.95$. We set the packet size to be 3600 bits and the time interval between two consecutive transmissions as 20 ms. This results in a maximum transmission bit rate of 180,000 bit/s. Clearly the numerical results scale correspondingly to networks with different transmission rates. Corresponding to the settings in numerical analysis, we perform simulation in Matlab. For different startup delay values and buffer sizes, we simulate the transmission and playback of each video sequence over 2000 realizations of the random VBR channel and measure the jitter free probability. Furthermore, we compute the upper and lower bounds of the jitter free probability based on the proposed analysis and compare them with the simulation results.

B. Effect of Initial Playback Delay

In Figure 7 we plot the jitter-free probability vs. startup delay value for video “Alpin Ski” with different fixed buffer sizes, including a case with infinite buffer size. Also indicated are the corresponding values of Δ_B , the highest supporting line of the buffer limit curve $p(t) + B$ as defined in (19). We observe that the derived upper bounds and lower bounds provide close estimation of the actual jitter free probability, especially within desired parameter ranges, where the startup delay is small to moderate and the jitter-free probability is high. Similar results are observed for different playback curves and omitted to reduce redundancy.

We note that, when $\Delta \leq \Delta_B$, the finite buffer case and the infinite buffer case are nearly the same, and the jitter free probability increases as Δ increases. This is because when $\Delta \leq \Delta_B$, as we can infer from Figure 4, $R(t)$ will always stay below $R_B(t)$, so there will not be any overflow, and jitter is only induced by underflow. A larger Δ reduces the probability of underflow. However, after Δ surpasses Δ_B , the jitter free probability first increases, but by only a very small amount, and then decreases as Δ increases. This is because when $\Delta > \Delta_B$, overflow occurs. And since the buffer size is fixed, a longer startup delay will result in accumulating too much data and hence increasing the probability of overflow. When Δ becomes larger, overflow starts to dominant and the jitter free probability goes to zero.

The practical implication of the above observation is clear. The initial playback delay is a delicate parameter in the optimal design of multimedia streaming. Increasing the initial playback delay can drastically improve the jitter-free probability, but only up to a point determined by the playback curve and the receiver buffer size. Beyond that point, increasing the initial playback delay can in fact significantly increase playback jittering. In this regard, the proposed analysis framework provides a means to accurately estimate the optimal value of the initial playback

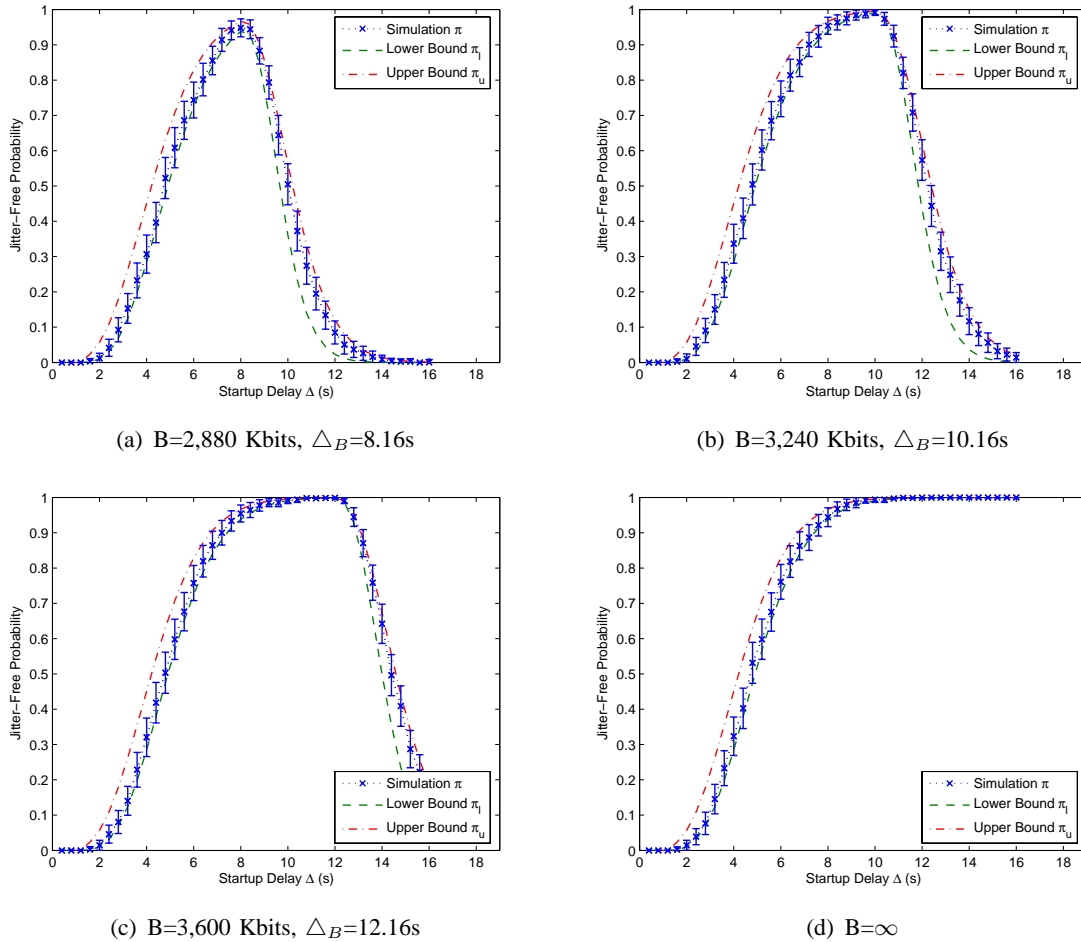


Fig. 7. Jitter free probability vs. startup delay with different receiver buffer sizes for video “Alpin Ski”. With 90% confidence intervals for 200 runs.

delay.

C. Effect of Receiver Buffer Size

Figure 8 shows the effect of receiver buffer size on the jitter-free probability for video “Alpin Ski” given different startup delay values. It can be seen in this figure that the jitter-free probability π increases quite fast as the buffer size B increases at first and then after B surpasses a certain value, π is approximately constant. Thus, increasing the receiver buffer will not necessarily result in drastically improved performance.

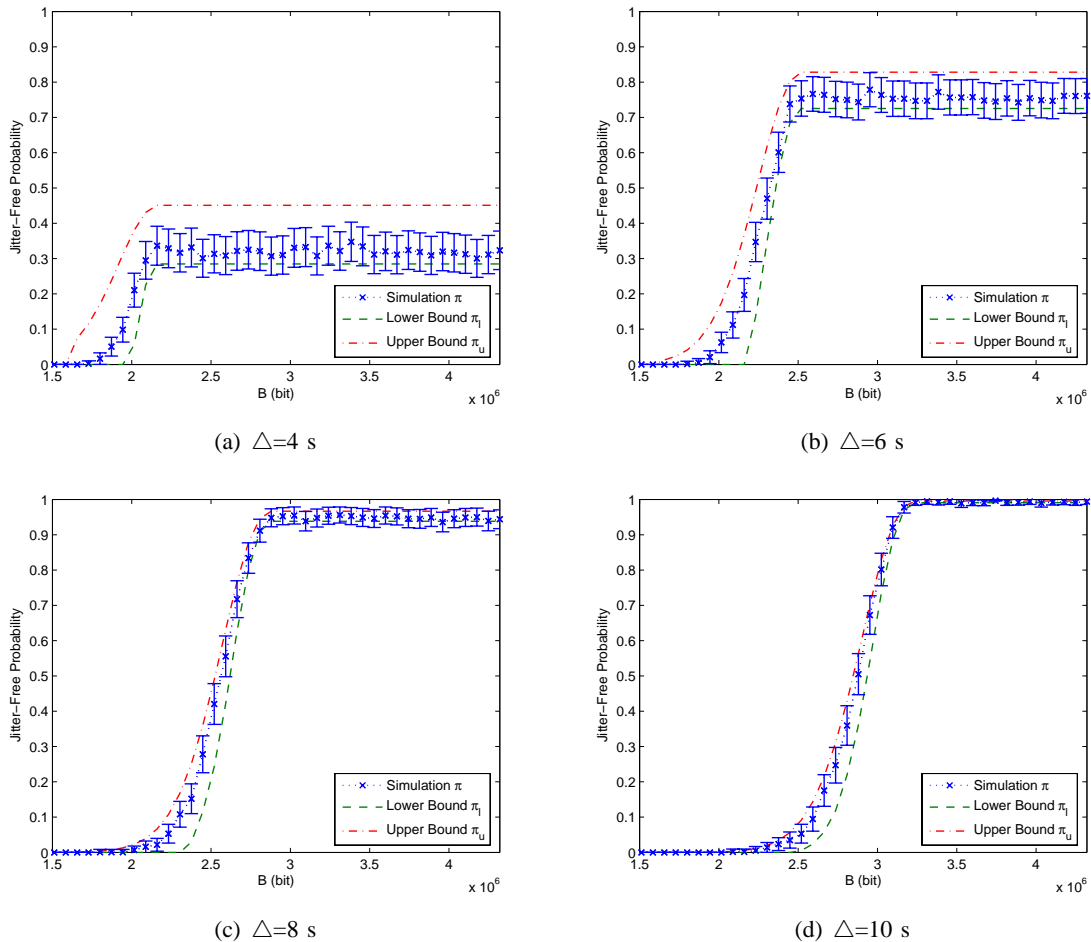


Fig. 8. Jitter free probability vs. buffer size with different startup delays for video “Alpin Ski”. With 90% confidence intervals for 200 runs.

Furthermore, we note that for a given initial delay Δ , there exists a maximum buffer size

$$B_{max}(\Delta) = \max_t \{ \min \{ b_{max}(t + \Delta), p(L) \} - p(t) \} \quad (38)$$

such that for any $B \geq B_{max}(\Delta)$, π is constant:

$$\pi = \Pr \{ R(t) \geq p(t) \ \forall t \leq L \}. \quad (39)$$

The idea is that since $R(t) \leq b_{max}(t + \Delta)$ for all t , if $R_B(t) \geq b_{max}(t + \Delta)$, overflow will not

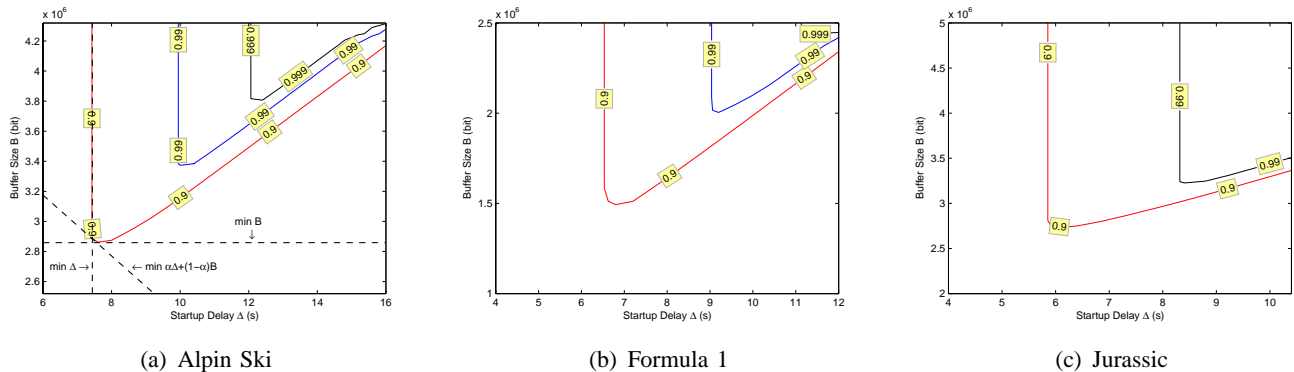


Fig. 9. Contour maps of buffer size vs. startup delay, with jitter-free probabilities labelled on the curves.

occur and only underflow contributes to jitter, which is equivalent to the infinite buffer case.

Clearly, in terms of resource allocation, hardware implementation, and energy consumption cost, a smaller buffer size is preferred in practice. Therefore, the proposed analytical framework, allowing numerical results such as those presented in Figure 8, can provide a means for a first step toward quantifying the most sensible buffer sizes for optimal system design, taking into consideration different system cost factors.

D. Optimal Delay-Buffer Tradeoff

Finally, we consider the optimal tradeoff between the initial playback delay Δ and the receiver buffer size B in jitter-free streaming. Figure 9 shows the contour maps of the startup delay and the buffer size that achieve different jitter free probabilities, for the three video clips described above.

We observe that the right branch of a contour curves have a slope roughly equal to b_{max} , the maximum transmission rate of the channel. This corresponds to the fact that as Δ increases, regardless the boundary effect, $B_{max}(\Delta)$ increase at rate b_{max} . This confirms our previous observation that, in order to achieve $\pi \rightarrow 1$ for a given delay Δ , we should have $B \rightarrow B_{max}(\Delta)$.

It is interesting to see in Figure 9 that all contours have a sharp turn at the left bottom and as a result all tangent lines with different values of α intersect with the contour curve all around the corner. This means the optimal operation point of different α 's are close to each other and every one is a sub-optimal solution to other values of α .

For different video traces, the shapes of the contour curves are similar except for a roughly constant shift almost equating the difference in Δ_{min} and B_{min} between the different videos. This suggests that for different videos, to achieve the same jitter free probability, one should choose the startup delay and buffer size roughly based on the values of the Δ_{min} and B_{min} of each video.

Finally, this figure provides a convenient means to obtain an optimal operating point for the system that balances the tradeoff between Δ and B , given a certain required jitter-free probability π . If we define a cost function as a weighted sum of the two

$$C = \alpha\Delta + (1 - \alpha)B, \quad (40)$$

where $\alpha \in [0, 1]$, then to minimize this cost function, we simply find the tangent line of the corresponding contour curve with slope $\frac{\alpha}{\alpha-1}$. The point of contact between the tangent line and the contour curve given a value of π defines the optimal operating point for the system. An illustration of such a procedure is shown in Figure 9.

VI. CONCLUSIONS

In this work, we evaluate the performance of VBR encoded media streaming over random VBR channels, by deriving upper and lower probability bounds for jitter-free streaming. We have shown that, when some statistical characteristics of the channel are available, jitter-free

streaming can be achieved with high probability by selecting appropriate initial playback delay values and receiver buffer sizes.

We have presented a novel analytical framework that only requires knowledge of the playback curve, the maximum channel bit rate, and general statistics of the channel, to derive the probability bounds for jitter-free streaming, for both the infinite buffer and finite buffer cases. We demonstrate the application of this analytical framework in a wireless access network with a general extended Gilbert model and ARQ error control. Numerical and experimental results using MPEG-4 encoded VBR video traces validate our findings.

The computed bounds allow precise estimation of the effects of initial playback delay and receiver buffer size on streaming performance, especially within system parameter ranges that lead to sensible jitter-free probabilities. To a practical streaming system designer, the proposed analysis technique provides a convenient framework to balance the tradeoffs between the initial playback delay, the receiver buffer size, and the jitter free probability for optimal VBR media streaming over random VBR channels.

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