# EC431H1 Digital Signal Processing FINAL EXAM April 26, 2004, 2:00 p.m. Instructor: D. Hatzinakos

#### **Instructions:**

- 1. Type A exam
- 2. Non-programmable calculators are allowed
- 3. Please solve all five problems. All problems are equally weighted.
- 4. All answers must be written in the examination booklet. Do not write any answers in this problem handout.

## PROBLEM 1 (10 points)

An A/D system converts by ideal sampling at 16kHz.



- (a) If a continuous time signal of the form  $x(t) = cos(2.8\pi 10^4 t + \pi/4)$  is sampled, sketch, with careful labeling of axes and impulses, the DTFT of the sequence x[n] = x(nT).
- (b) A reconstruction is made by interpolating the samples according to

with 
$$T$$
 as in part (a) and  $sinc(t) = sin(\pi t)/\pi t$ . Find  $y(t)$  in its simplest form.

(c) The signal y(t) of (b) is not the same as the x(t) we sampled in (a). You are restricted to using the interpolator as in part (b), but now you may use a linear discrete time filter to process x[n] before reconstructing. The goal is to make the reconstructed signal  $\hat{x}(t)$  identical to x(t). In other words, you will create  $\tilde{x}[n] = \sum_{-\infty}^{\infty} x(m)h(n-m)$ , then reconstruct

$$\hat{x}(t) = \sum_{-\infty}^{\infty} \tilde{x}[n] sinc\left(\frac{2t - nT}{T}\right)$$

with T fixed as above. Design an FIR filter to achieve this, or show why you cannot do it.

DO NOT WRITE IN THIS SPACE

be y(t) = Acos (2.10)2+t

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+ B cos (14.103 20++

#### PROBLEM 2 (10 points)

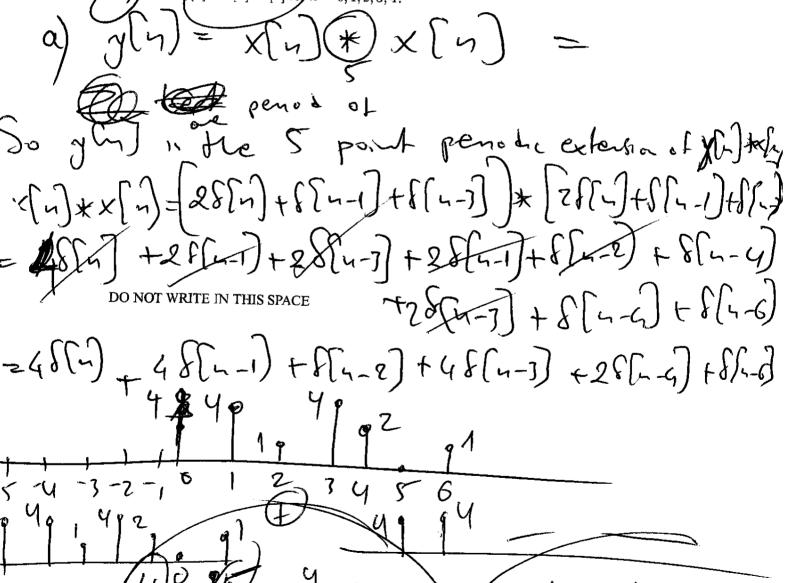
Consider the finite length sequence

$$x[n] = 2\delta[n] + \delta[n-1] + \delta[n-3]$$

We perform the following operation on this sequence:

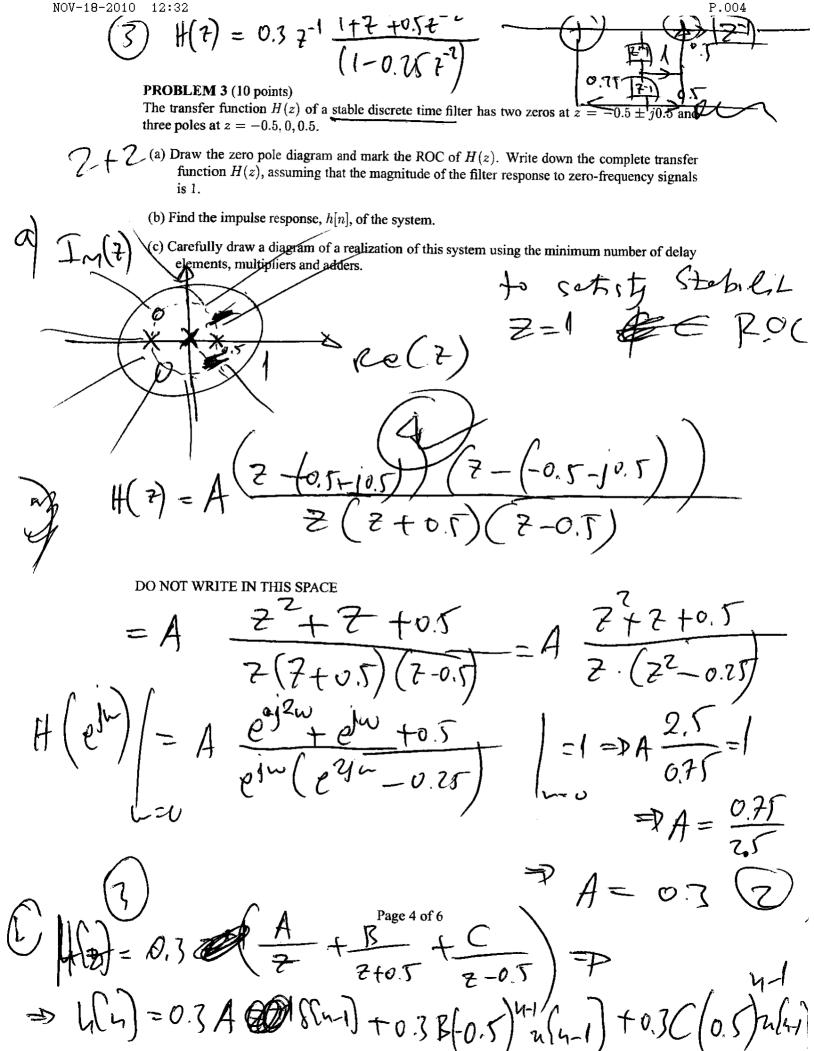
- (i) We compute the five-point DFT X[k]
- (ii) We compute a five-point inverse DFT of  $Y[k] = X^2[k]$  to obtain a sequence y[n].
  - a) Determine the sequence y[n] for n = 0, 1, 2, 3, 4.
  - b) if N point DFTs are used in the two step procedure, how should we choose N so that

f[n] = x[n] \* x[n] for f[n] = 0, 1, 2, 3, 4?



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+ 58[n-1]+8[n-2]+4[[n-7]+



## PROBLEM 4 (10 points)

A designer has available a number of six-point FFT chips. Show explicitly how he/she should interconnect two such chips to compute a twelve-point DFT. What is the number of multiplications

