

Midterm exam 2022, Solutions

Student name:
Student number:

bit budget = 35 bits

①

20	10	16	7
-10	5	4	3
17	6	3	-1
-20		20	

Note: This is a 1 level WT. Therefore there are no parents ~~pixels~~ and descendants pixels

$$T_0 = 16 = 2^4$$

first pass: sp 12 12 12 sp 12 12 12 sp 12 12 12 12 12 12 12 12 32 bits

$$1.5 T_0 = 24$$

24	0	24	0
0	0	0	0
24	0	0	0
0	0	0	0

→ Correction: $\begin{cases} 20 - 24 < 0 \\ 16 - 24 < 0 \\ 17 - 24 < 0 \end{cases} - \frac{T_0}{4} =$

$\frac{T_0}{4} = 4$ 3 bits

20	0	20	0
0	0	0	0
20	0	20	0
0	0	0	0

total of 35 bits stop here.

full bit stream: 11 01 01 01 11 01 01 01 11 01 01 01 01 01 01 01 01 01

② Original image $G = (A^H F A)$

$$\frac{1}{\sqrt{2}} \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & -1 \end{bmatrix} \begin{bmatrix} 20 & 10 & 16 & 7 \\ -10 & 5 & 4 & 3 \\ 17 & 6 & 3 & -1 \\ -20 & & 20 & \end{bmatrix} \frac{1}{\sqrt{2}} \begin{bmatrix} 11 & 00 \\ 00 & 11 \\ 1 & -1 & 00 \\ 00 & 1 & -1 \end{bmatrix} = \frac{1}{2} \begin{bmatrix} 56 & 18 & 22 & 10 \\ 10 & -10 & 12 & -4 \\ -6 & 18 & 0 & 22 \\ -6 & -10 & 8 & 2 \end{bmatrix}$$

permutation is

$$A^H \begin{bmatrix} 20 & 0 & 20 & 0 \\ 0 & 0 & 0 & 0 \\ 20 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} A = \begin{bmatrix} 10 & 10 & 0 & 0 \\ 10 & -10 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

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$$(3) \quad b_k = R \left(1 + \log_2 \frac{w_k G_k^2}{\prod_{i=1}^4 (w_i G_i^2)^{a_i}} \right)$$

Here $a_1 = a_2 = a_3 = a_4 = \frac{1}{4}$, $w_k > 1$ all k

So we need to calculate G_k^2 , $k=1, 2, 3, 4$
 from each subband $G_k^2 = E\{X^2\} - (E\{X\})^2 = \frac{1}{4} \sum_{i=1}^4 x_i^2 - \left(\frac{1}{4} \sum_{i=1}^4 x_i \right)^2$

$$\text{So for } G_1^2 = \frac{1}{4} (20^2 + 10^2 + (-10)^2 + 5^2) - \left(\frac{1}{4} (20 + 10 - 10 + 5) \right)^2$$

$$= 117.14$$

Similarly

$$G_2^2 = 26.25$$

$$G_3^2 = 54.7$$

$$G_4^2 = 2.5$$

Then $b_1 \approx 3$ bits

$$b_2 = 0.276 \text{ bits}$$

$$b_3 = 0.376$$

$$b_4 = 1 + \log_2 0.1 < 0 = 0$$

$$R = \frac{1}{4} (3 + 0.276 + 0.376) = 1$$

- ④ H.261 has I and P frames
H.263 has I, P, B frames, ———

⑤ Video coding explores both spatial and temporal redundancy

⑥ $\frac{N}{2} \times \frac{N}{2}$ largest subband

$\frac{N}{2^5} \times \frac{N}{2^5}$ smallest subband

$3 \times 5 + 1 = 16$ total # of subbands

⑦ⁱⁿ Asymmetrical coding the decoder is well defined while the encoder can have arbitrarily high sophistication and complexity

MPEG is asymmetrical

H.261 is symmetrical

⑧ Assume 30 frames/sec $N \times N$ pixels

Then bit rate is $30 \times 3 \times N \times N \times 8 = \dots$