

Cloud Radio-Access Networks: Capacity, Coding Strategies, and Optimization

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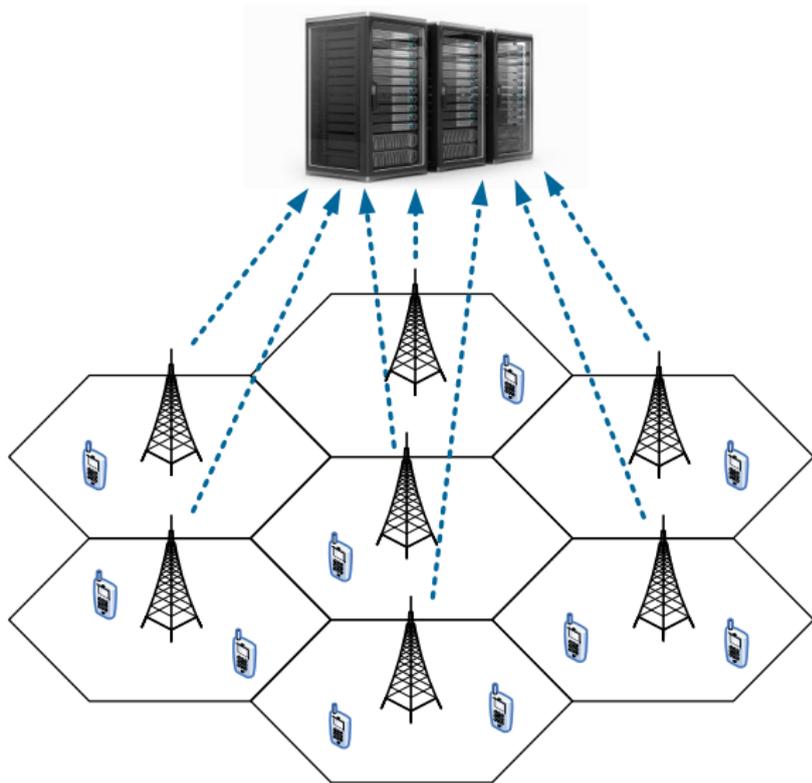
Joint work with Binbin Dai, Pratik Patil, Yuhan Zhou, Liang Liu

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- Future 5G wireless cellular network:
 - Requirements: Gbps capacity, 1ms latency, 10^5 connectivity
 - Bottleneck: Path-loss, fading, and interference
- Emerging trends:
 - Dense
 - Heterogeneous network; Small cell
 - Massive
 - Massive MIMO at each BS
 - Cooperative
 - Signal processing for interference cancellation
- This talk: Capacity and optimization of cooperative networks.

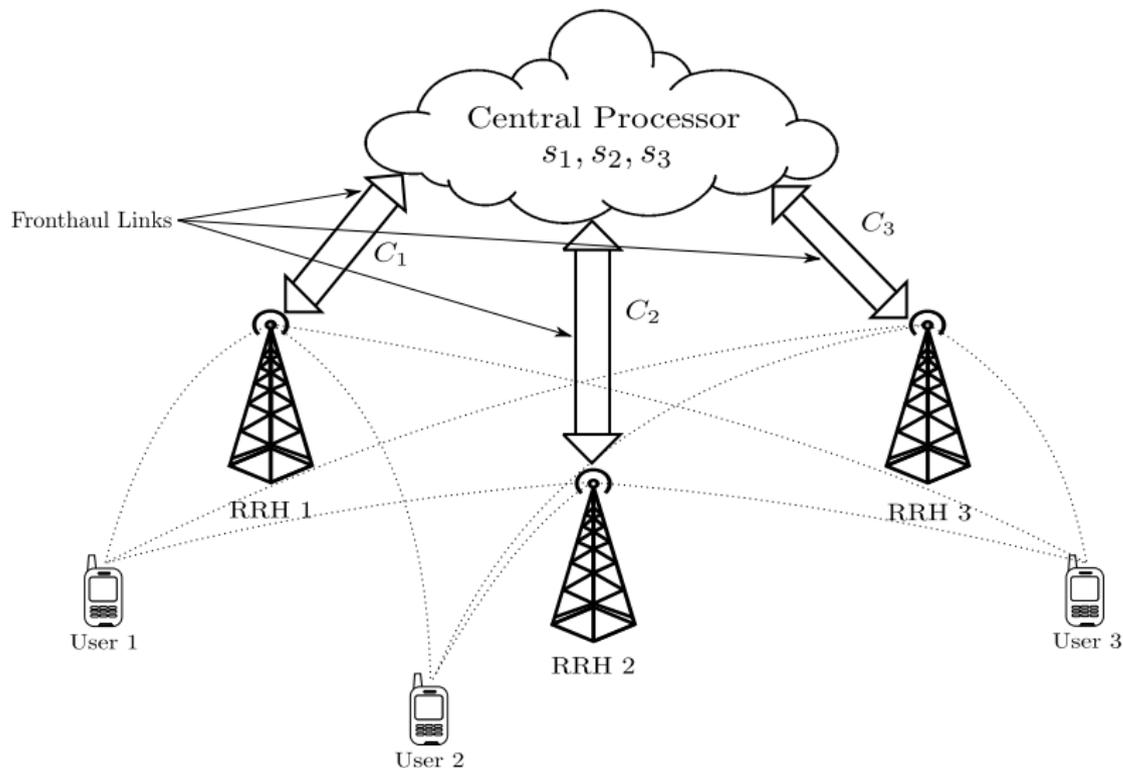
Cooperating BSs in the Cloud



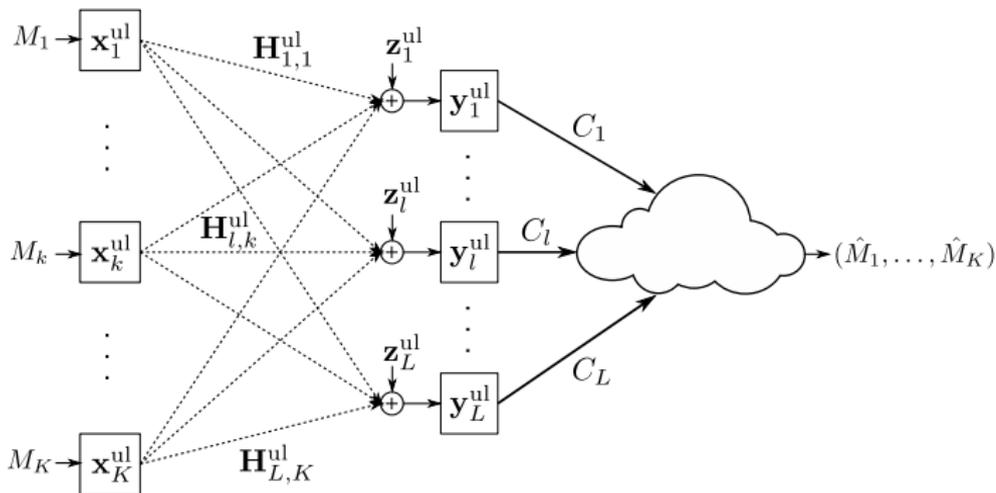
Cloud Radio-Access Network (C-RAN)

- Benefits of C-RAN:
 - ◇ Allows a cost-effective way to deploy and upgrade wireless platform;
 - ◇ Opens up new possibilities for the optimization of air-interface;
 - ◇ Enables cooperative communication for interference mitigation;
 - ◇ Provides an implementation of coordinated multi-point (CoMP).
- This talk: Information theoretical analysis of C-RAN
 - ◇ Multicell Joint Processing for Uplink C-RAN
 - ◇ Multicell Beamforming for Downlink C-RAN

Wireless Access via the Cloud

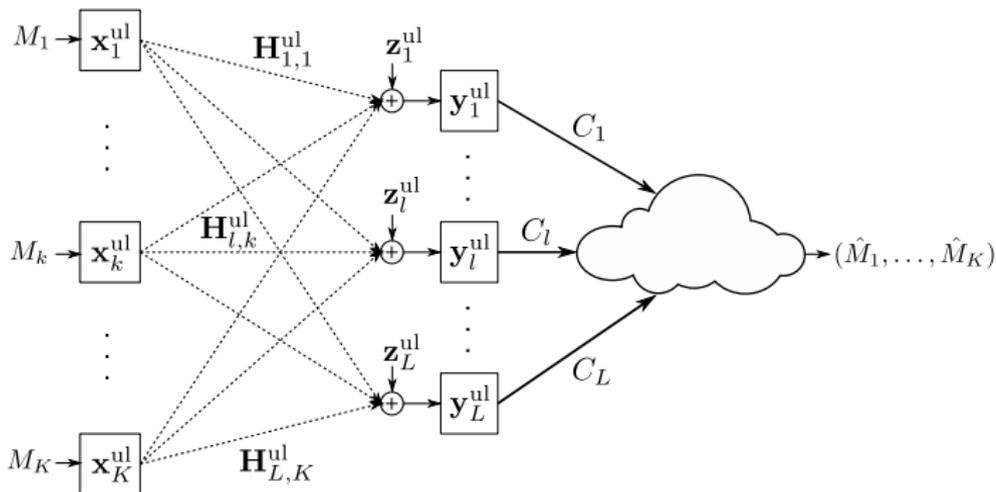


Uplink Multicell Joint Processing



- X_1, X_2, \dots, X_K are user terminals; Y_1, Y_2, \dots, Y_L are RRHs.
- Practical constraint: Fronthaul capacity limited to C_l .
- Goal: To maximize the overall capacities for all users.

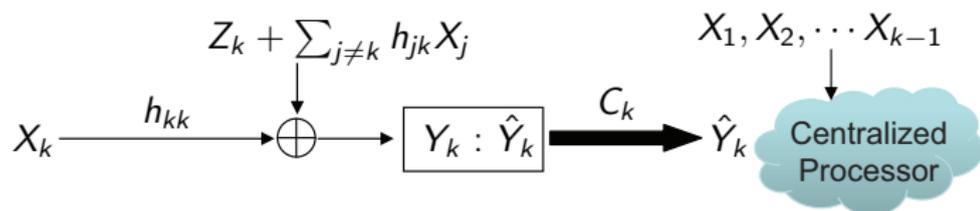
Distributed Detection in Uplink C-RAN



- What should each RRH do? Local detection vs. compression...
- What should the cloud do? Successive vs. joint decoding...
- How should we design transmit signaling?

Successive Interference Cancellation in the Cloud

Equivalent channel of user k in the k^{th} decoding stage:



- The quantized observation at RRH k is sent to the centralized processor via the fronthaul link of rate C_k .
- Previously decoded X_1 to X_{k-1} serve as side information for Wyner-Ziv compression and for decoding of X_k , achieving:

$$R_k = \frac{1}{2} \log \frac{1 + \overline{\text{SINR}}_k}{1 + 2^{-2C_k} \overline{\text{SINR}}_k}$$

where $\overline{\text{SINR}}_k = (h_{kk}^2 P_k) / (N_0 + \sum_{j > k} h_{jk}^2 P_j)$

- Per-RRH decoding with SIC:

$$R_k = I(X_k; \hat{Y}_k | X_1, \dots, X_{k-1})$$

subject to $I(Y_k; \hat{Y}_k | X_1, \dots, X_{k-1}) \leq C_k$.

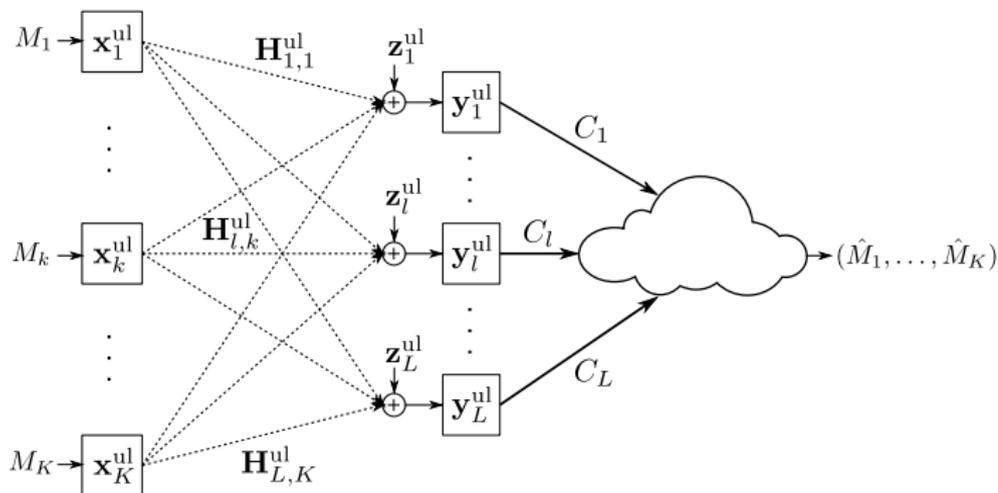
- Joint-RRH decoding can do better:

$$R_k = I(X_k; \hat{Y}_1, \dots, \hat{Y}_L | X_1, \dots, X_{k-1}),$$

subject to $I(Y_k; \hat{Y}_k | \hat{Y}_1, \dots, \hat{Y}_{k-1}) \leq C_k$.

- Each RRH compresses Y_i into \hat{Y}_i
 - Compression can be done with Wyner-Ziv or single-user coding.
- The cloud decodes the quantized received signals $\{\hat{Y}_1, \dots, \hat{Y}_L\}$, then the transmit messages X_1, X_2, \dots, X_K , successively or jointly.
- Information theoretical justification:
 - Joint decoding proposed by Sanderovich-Somekh-Poor-Shamai ('09) and Sanderovich-Shamai-Steinberg-Kramer ('08)
 - Avestimehr-Diggavi-Tse ('09): "Wireless Network Info Flow"
 - Lim-Kim-El Gamal-Chung ('11): "Noisy Network Coding"

Optimality of Gaussian Signaling and Quantization



- Fact: Assuming Gaussian quantization, optimal input is Gaussian.
- Theorem: Assuming Gaussian input, optimal quantizer is Gaussian.
- However, joint Gaussian signal/quantization may not be optimal
 - Binary counterexample: Sanderovich-Shamai-Steinberg-Kramer'08

Theorem (Achievable rate region)

Achievable rate under sum fronthaul constraint C :

$$\sum_{i \in \mathcal{S}} R_i \leq \log \frac{|\mathbf{H}_S \mathbf{K}_X(s) \mathbf{H}_S^H + \Lambda_q + \sigma^2 \mathbf{I}|}{|\Lambda_q + \sigma^2 \mathbf{I}|}$$

either subject to (for Wyner-Ziv coding, V-MAC-WZ):

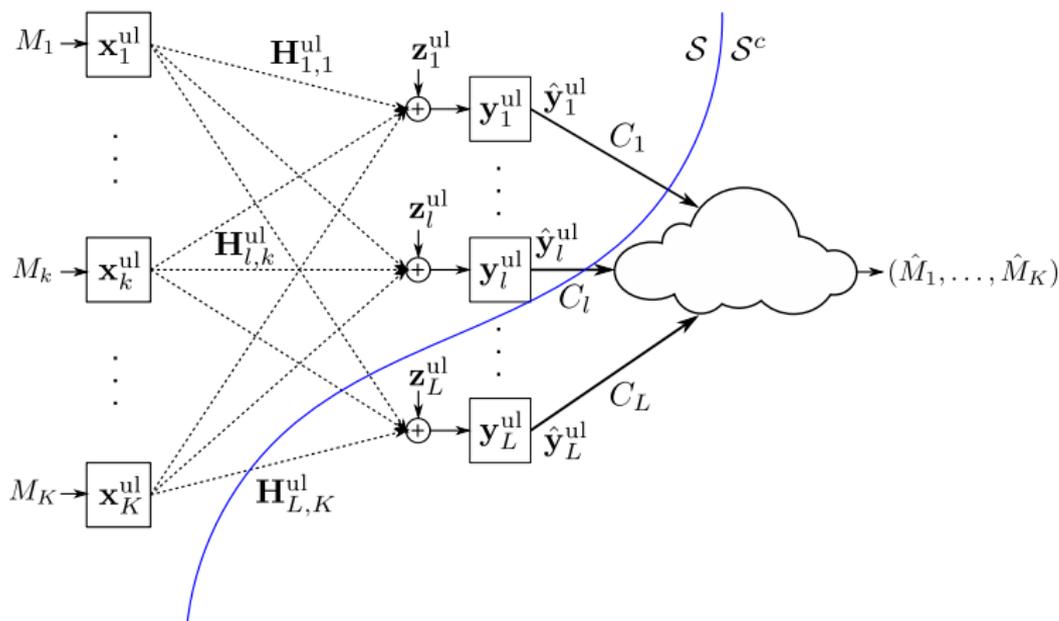
$$\log \frac{|\mathbf{H} \mathbf{K}_X \mathbf{H}^H + \Lambda_q + \sigma^2 \mathbf{I}|}{|\Lambda_q|} \leq C$$

or subject to (for single-user compression, V-MAC-SU):

$$\log \frac{|\text{diag}(\mathbf{H} \mathbf{K}_X \mathbf{H}^H) + \Lambda_q + \sigma^2 \mathbf{I}|}{|\Lambda_q|} \leq C$$

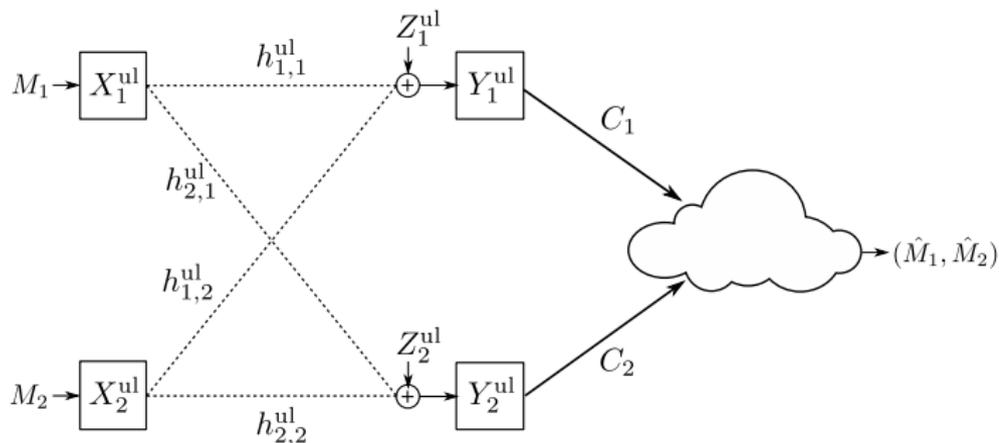
where $\Lambda_q = \text{diag}(q_1, q_2, \dots, q_L)$ is the quantization noise level.

Noisy Network Coding (Lim-Kim-El Gamal-Chung'11)



- Cut-set Bound: $R(\mathcal{S}) = \sum_{k \in \mathcal{S}} R_k \leq I(\mathbf{x}^{\text{ul}}(\mathcal{S}); \mathbf{y}^{\text{ul}}(\mathcal{S}^c) | \mathbf{x}^{\text{ul}}(\mathcal{S}^c))$
- Achievable rate using noisy network coding: $R(\mathcal{S}) \leq I(\mathbf{x}^{\text{ul}}(\mathcal{S}); \hat{\mathbf{y}}^{\text{ul}}(\mathcal{S}^c), \mathbf{y}_d^{\text{ul}} | \mathbf{x}^{\text{ul}}(\mathcal{S}^c)) - I(\mathbf{y}^{\text{ul}}(\mathcal{S}); \hat{\mathbf{y}}^{\text{ul}}(\mathcal{S}) | \mathbf{x}_{\text{ul}}^{\text{ul}}(\mathcal{S}), \hat{\mathbf{y}}^{\text{ul}}(\mathcal{S}^c), \mathbf{y}_d^{\text{ul}})$
- Set quantization noise at background noise level: $\hat{\mathbf{y}}_k^{\text{ul}} \approx \mathbf{y}_k^{\text{ul}}$.

Approximate Optimality of Compress-and-Forward



Successive-decoding region for MAC

$$R_1 < I(X_1^{\text{ul}}, \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_2^{\text{ul}});$$

$$R_2 < I(X_2^{\text{ul}}, \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_1^{\text{ul}});$$

$$R_1 + R_2 < I(X_1^{\text{ul}}, X_2^{\text{ul}}, \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}})$$

Wyner-Ziv Compression

$$C_1 > I(Y_1^{\text{ul}}, \hat{Y}_1^{\text{ul}} | \hat{Y}_2^{\text{ul}});$$

$$C_2 > I(Y_2^{\text{ul}}, \hat{Y}_2^{\text{ul}} | \hat{Y}_1^{\text{ul}});$$

$$C_1 + C_2 > I(Y_1^{\text{ul}}, Y_2^{\text{ul}}, \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}})$$

Comparing with Noisy Network Coding

$$R_1 < I(X_1^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_2^{\text{ul}});$$

$$R_1 < I(X_1^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_2^{\text{ul}}) + C_1 - I(Y_1^{\text{ul}}; \hat{Y}_1^{\text{ul}} | \hat{Y}_2^{\text{ul}}, X_2^{\text{ul}});$$

$$R_1 < I(X_1^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_2^{\text{ul}}) + C_2 - I(Y_2^{\text{ul}}; \hat{Y}_2^{\text{ul}} | \hat{Y}_1^{\text{ul}}, X_2^{\text{ul}});$$

$$R_1 < I(X_1^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_2^{\text{ul}}) + C_1 + C_2 - I(Y_1^{\text{ul}}, Y_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_2^{\text{ul}});$$

$$R_2 < I(X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_1^{\text{ul}});$$

$$R_2 < I(X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_1^{\text{ul}}) + C_1 - I(Y_1^{\text{ul}}; \hat{Y}_1^{\text{ul}} | \hat{Y}_2^{\text{ul}}, X_1^{\text{ul}});$$

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$$R_2 < I(X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_1^{\text{ul}}) + C_1 + C_2 - I(Y_1^{\text{ul}}, Y_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}} | X_1^{\text{ul}});$$

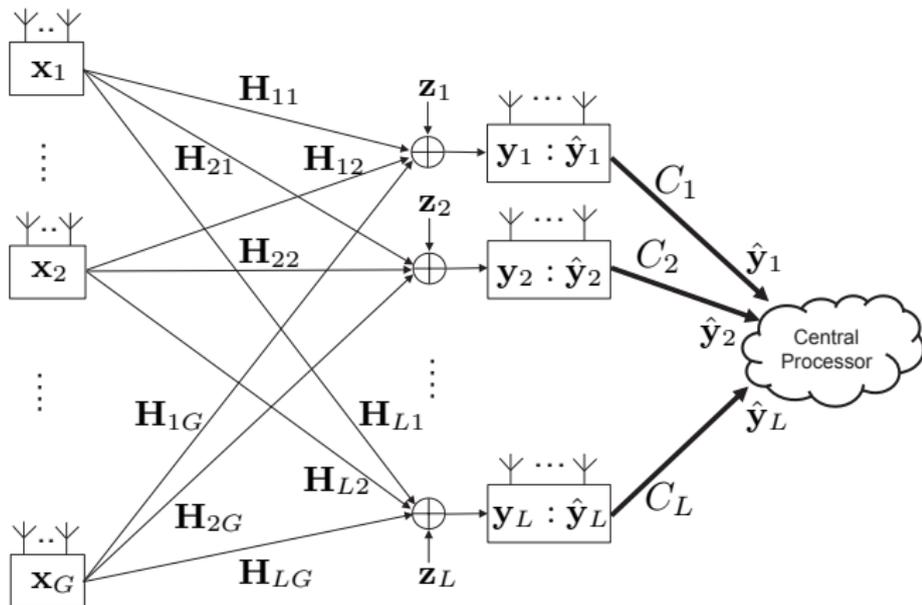
$$R_1 + R_2 < I(X_1^{\text{ul}}, X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}});$$

$$R_1 + R_2 < I(X_1^{\text{ul}}, X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}}) + C_1 - I(Y_1^{\text{ul}}; \hat{Y}_1^{\text{ul}} | \hat{Y}_2^{\text{ul}});$$

$$R_1 + R_2 < I(X_1^{\text{ul}}, X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}}) + C_2 - I(Y_2^{\text{ul}}; \hat{Y}_2^{\text{ul}} | \hat{Y}_1^{\text{ul}});$$

$$R_1 + R_2 < I(X_1^{\text{ul}}, X_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}}) + C_1 + C_2 - I(Y_1^{\text{ul}}, Y_2^{\text{ul}}; \hat{Y}_1^{\text{ul}}, \hat{Y}_2^{\text{ul}})$$

Uplink C-RAN with Multiple Antennas



- Uniform quantization noise level is optimal only at high SQNR.
- In general: Jointly optimize transmit and quantization covariances.
- Solution: Successive convex approximation with WMMSE.
- WMMSE-SCA: Optimal Tx/Rx beamforming then compression.

Simulation Result: V-MAC-WZ

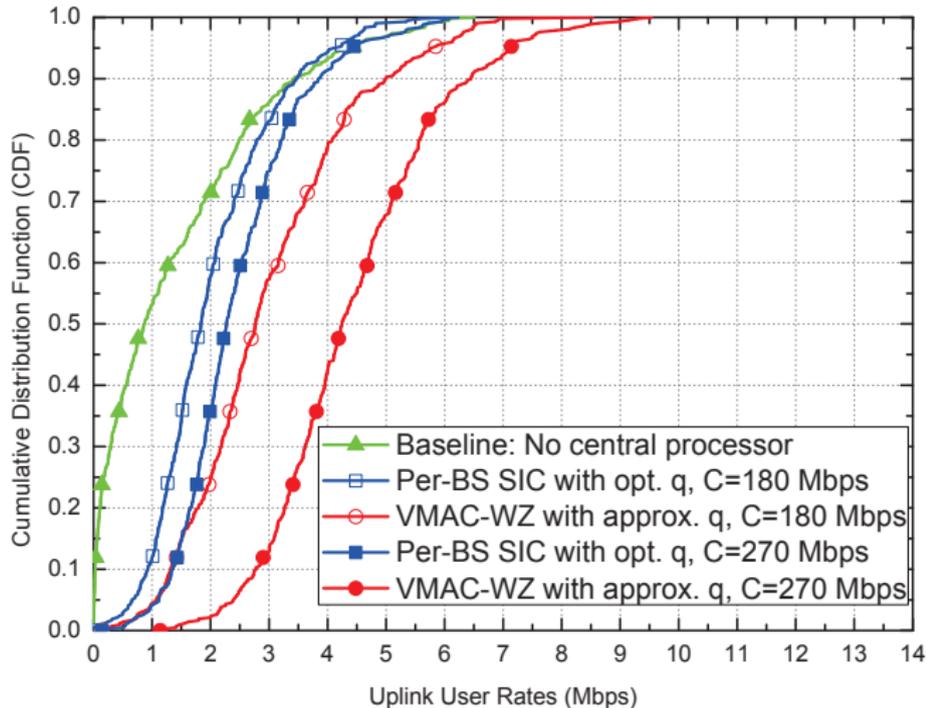


Figure: CDF of user rates in a 7-cell cluster: V-MAC-WZ vs. Per-BS SIC.

Simulation Result: Sum-Rate vs Backhaul

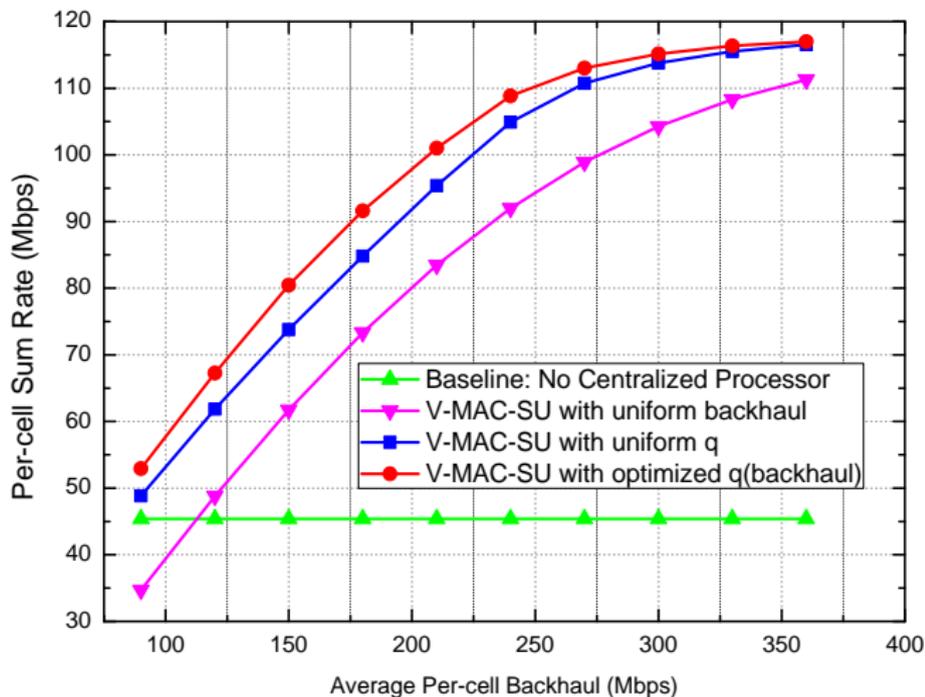


Figure: Per-cell sum rate vs. average per-cell fronthaul capacity.

Benefit of Beamform-Compress-Forward

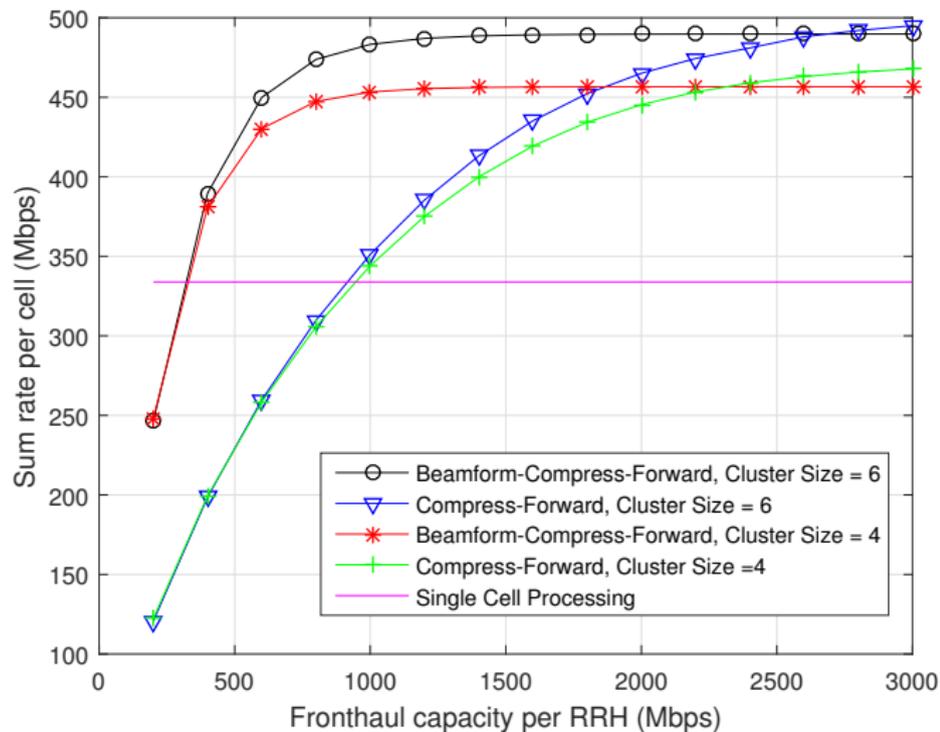
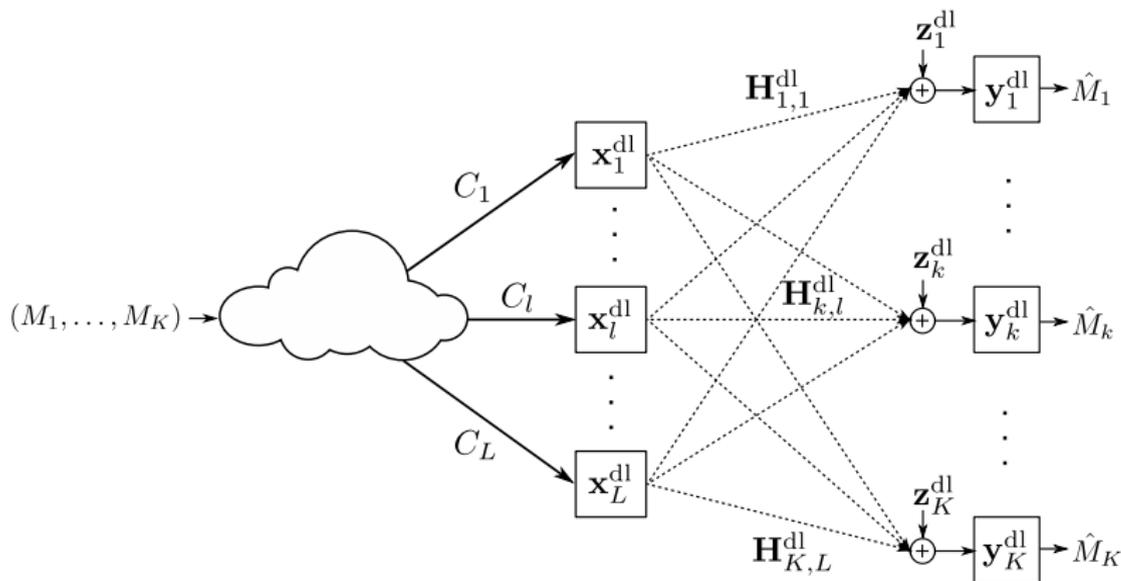


Figure: 12-antenna RRH serving 2 users: Compress vs. Beamform-Compress.

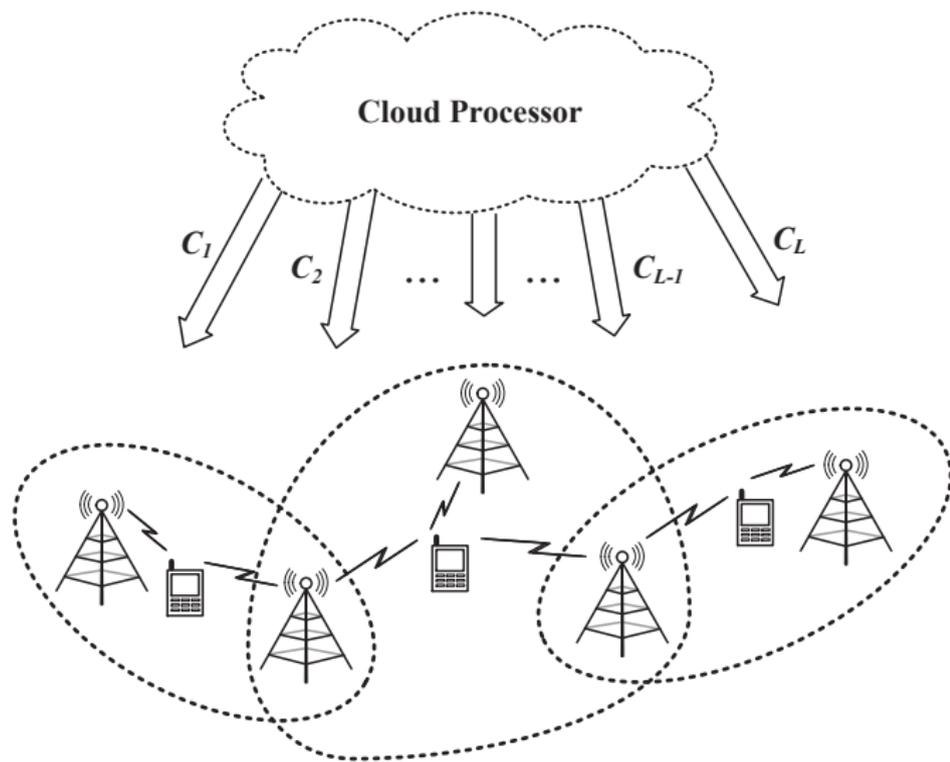
Downlink C-RAN as a Broadcast Relay Channel



- How to enable cooperation across clusters of RRHs?
 - Message-sharing with a cluster of RRHs for joint beamforming.
 - Precode at the cloud. Compress-forward precoded signals to RRHs.
 - Multivariate compression [Park-Simeone-Sahin-Shamai '13].

- Two fundamental coding strategies for downlink C-RAN:
 - *Data-Sharing*: CP distributes each user's data to a cluster of RRHs. Each RRH has access to multiple data streams then precodes.
 - *Compression*: CP computes the beamformer, then compresses and distributes the precoded signal to the RRHs.
- How to best utilize the limited fronthaul?
 - In *Data-Sharing*, limit the cluster size;
 - In *Compression*, control quantization level.

Optimizing Clustering in Message-Sharing



"Personalized" cloud

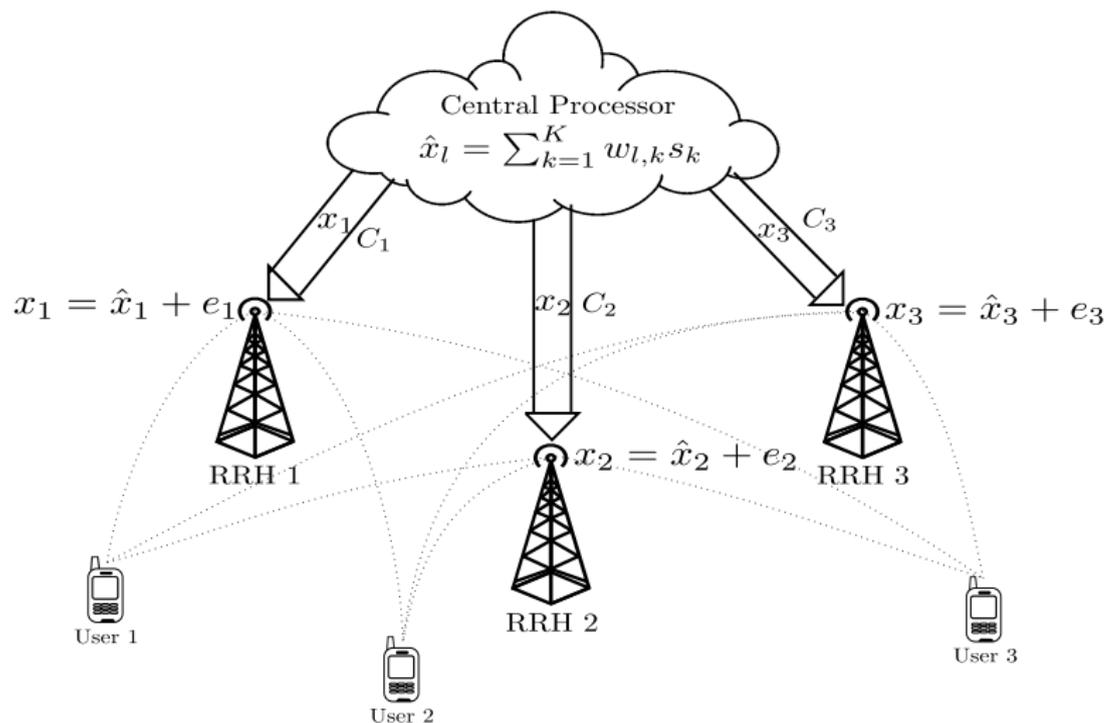
Sparse Beamforming for the Downlink C-RAN

- Weighted sum-rate maximization under per-RRH power constraints and per-RRH fronthaul constraints assuming single-stream per user:

$$\begin{aligned} & \text{maximize} && \sum_k \alpha_k R_k \\ & \text{subject to} && \sum_k \|w_k^l\|_2^2 \leq P_l, \forall l \\ & && \sum_k \left\| \|w_k^l\|_2^2 \right\|_0 R_k \leq C_l, \forall l \end{aligned}$$

- Use ℓ_1 re-weighting and compressed sensing [Candès-Wakin-Boyd'08]
- The **WMMSE** approach can be used to find a local optimum. [Christensen-Agarwal-Carvalho-Cioffi '08], [Shi-Razaviyayn-Luo-He '11], [Kaviani-Simeone-Krzymien-Shamai '12]
- Related work: Zhao-Quek-Lei ('13), Luo-Zhang-Lim ('14), Zhuang-Lau ('14),

Better Strategy: Compression for Multicell Beamforming



- Full cooperation possible, but compression introduces quantization noises.
- Optimizing by majorization-minimization: [Park-Simeone-Sahin-Shamai '13]

- Precoded signals intended for RRHs formed at central processor:

$$\hat{\mathbf{x}} = [\hat{x}_1, \dots, \hat{x}_L]^T = \sum_{k=1}^K \mathbf{w}_k s_k$$

- Quantization for $\hat{\mathbf{x}}$ modeled as $\mathbf{x} = \hat{\mathbf{x}} + \mathbf{e}$, where \mathbf{e} is the quantization noise with covariance \mathbf{Q} , independent of $\hat{\mathbf{x}}$.
- Achievable rate for user k is

$$R_k = \log \left(1 + \frac{|\mathbf{h}_k^H \mathbf{w}_k|^2}{\sum_{j \neq k} |\mathbf{h}_k^H \mathbf{w}_j|^2 + \sigma^2 + |\mathbf{h}_k^H \mathbf{Q} \mathbf{h}_k|} \right)$$

- The fronthaul capacity constraint must satisfy

$$\log \left(1 + \frac{\sum_{k=1}^K |w_{l,k}|^2}{q_l} \right) \leq C_l$$

Here, \mathbf{Q} is assumed diagonal; multivariate \mathbf{Q} also possible.

Data-Sharing vs. Compression for Downlink C-RAN

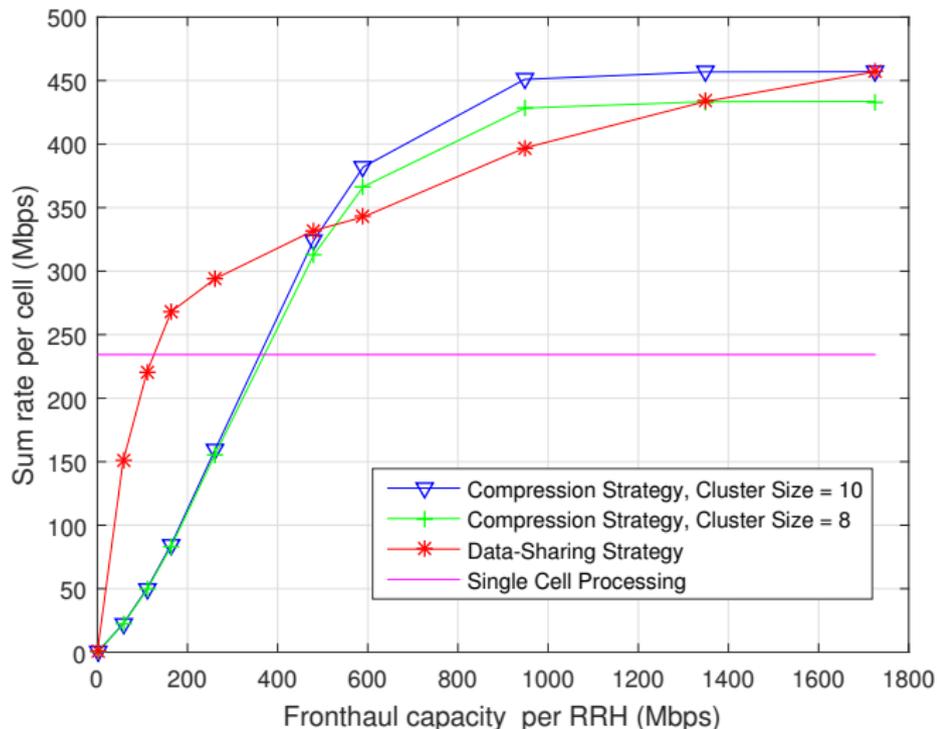
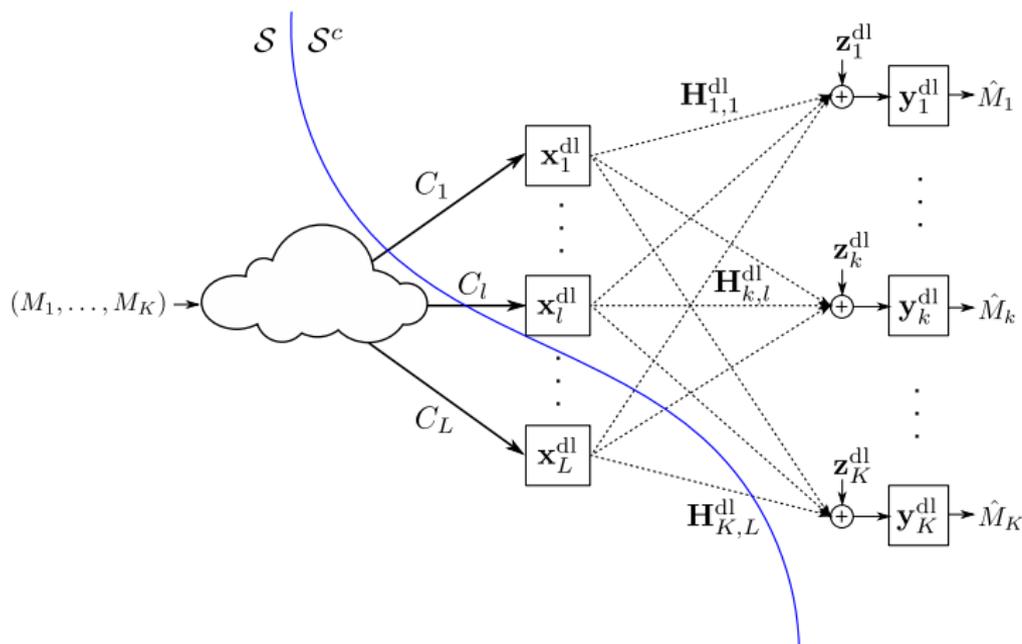


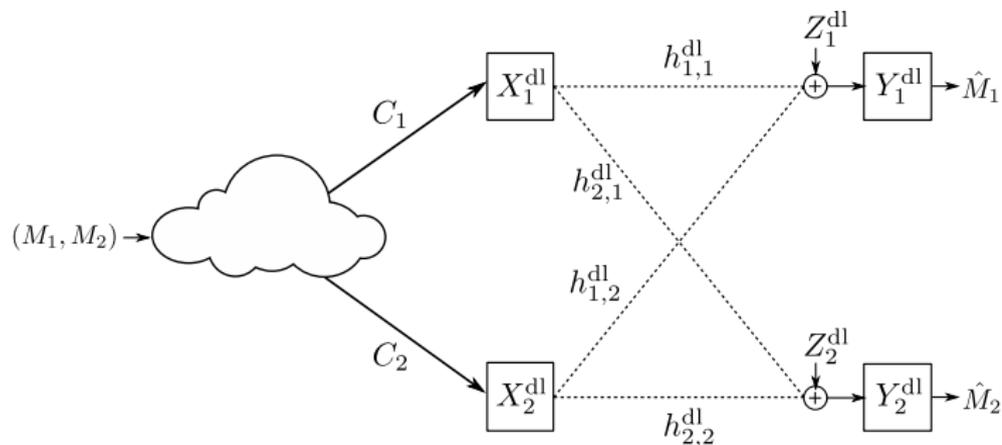
Figure: 4-antenna RRH with Independent Compression.

Distributed Decode-Forward (Lim-Kim-Kim'15)



- Cut-Set: $R(S) \leq I(x^{\text{dl}}(S); y^{\text{dl}}(S^c) | x^{\text{dl}}(S^c))$
- Distributed Decode-Forward: $R(S) \leq I(x^{\text{dl}}(S); \mathbf{u}(S^c) | x^{\text{ul}}(S^c)) - \sum_{k \in S^c} [I(\mathbf{u}_k^{\text{dl}}; \mathbf{u}(S_k^c), x_{\text{dl}}^{\text{N}} | x_k^{\text{dl}}, y_k^{\text{dl}}) + I(x_k^{\text{dl}}; x^{\text{dl}}(S_k^c))]$
- To achieve constant gap: Choose \mathbf{u}_k close to \mathbf{y}_k^{dl} .

Approximate Optimality of Compression-like Strategy



Marton's Region for Broadcast

$$R_1 < I(U_1; Y_1^{\text{dl}})$$

$$R_2 < I(U_2; Y_2^{\text{dl}})$$

$$R_1 + R_2 < I(U_1; Y_1^{\text{dl}}) + I(U_2; Y_2^{\text{dl}}) \\ - I(U_1; U_2);$$

Correlated Compression

$$C_1 > I(X_1^{\text{dl}}; U_1, U_2);$$

$$C_2 > I(X_2^{\text{dl}}; U_1, U_2);$$

$$C_1 + C_2 > I(X_1^{\text{dl}}, X_2^{\text{dl}}; U_1, U_2) \\ + I(X_1^{\text{dl}}; X_2^{\text{dl}})$$

Comparing with Distributed Decode-Forward

$$R_1 < I(U_1, Y_1^{\text{dl}});$$

$$R_1 < I(U_1, Y_1^{\text{dl}}) + C_1 - I(U_1; X_1^{\text{dl}});$$

$$R_1 < I(U_1, Y_1^{\text{dl}}) + C_2 - I(U_1; X_2^{\text{dl}});$$

$$R_1 < I(U_1, Y_1^{\text{dl}}) + C_1 + C_2 - I(U_1; X_1^{\text{dl}}, X_2^{\text{dl}});$$

$$R_2 < I(U_2, Y_2^{\text{dl}});$$

$$R_2 < I(U_2, Y_2^{\text{dl}}) + C_1 - I(U_2; X_1^{\text{dl}});$$

$$R_2 < I(U_2, Y_2^{\text{dl}}) + C_2 - I(U_2; X_2^{\text{dl}});$$

$$R_2 < I(U_2, Y_2^{\text{dl}}) + C_1 + C_2 - I(U_2; X_1^{\text{dl}}, X_2^{\text{dl}});$$

$$R_1 + R_2 < I(U_1, Y_1^{\text{dl}}) + I(U_2, Y_2^{\text{dl}}) - I(U_1; U_2);$$

$$R_1 + R_2 < I(U_1, Y_1^{\text{dl}}) + I(U_2, Y_2^{\text{dl}}) - I(U_1; U_2) + C_1 - I(U_1, U_2; X_1^{\text{dl}});$$

$$R_1 + R_2 < I(U_1, Y_1^{\text{dl}}) + I(U_2, Y_2^{\text{dl}}) - I(U_1; U_2) + C_2 - I(U_1, U_2; X_2^{\text{dl}});$$

$$R_1 + R_2 < I(U_1, Y_1^{\text{dl}}) + I(U_2, Y_2^{\text{dl}}) - I(U_1; U_2) + C_1 + C_2 - I(U_1, U_2; X_1^{\text{dl}}, X_2^{\text{dl}}) \\ - I(X_1^{\text{dl}}; X_2^{\text{dl}})$$

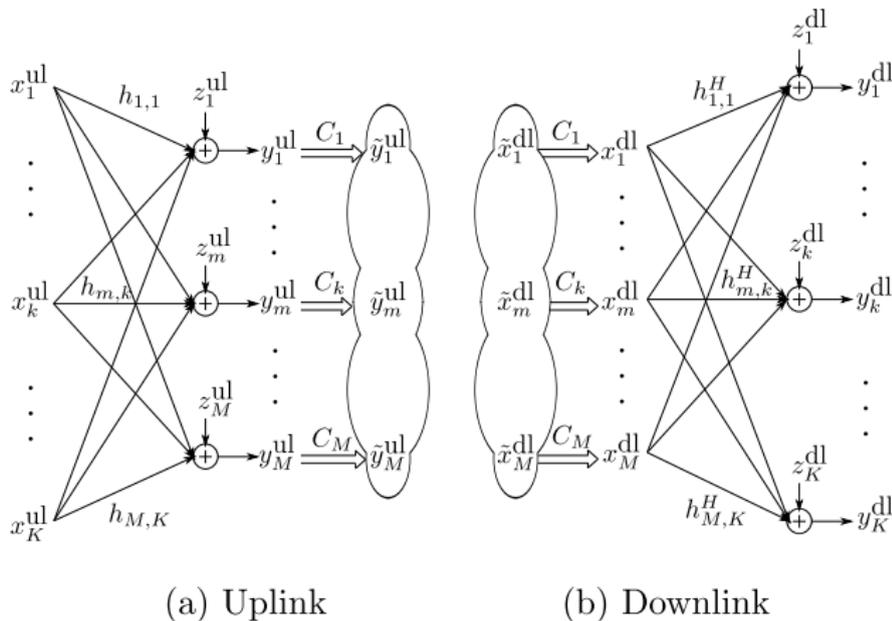
Uplink

- Multiple-access-relay channel
- Simple encoders, complex cloud decoder
- Compress-forward with independent or Wyner-Ziv compression
- Noisy network coding within constant gap

Downlink

- Broadcast-relay channel
- Simple decoders, complex cloud encoder
- Compression strategy with independent or multivariate compression covering
- Distributed decode-forward within constant gap

Uplink-Downlink Duality in C-RAN



- Uplink-downlink duality for compression-based beamforming
 - Under same sum-power and individual fronthaul constraints.
 - Achievable rates of the uplink and downlink are the same.
- Generalization of uplink-downlink duality to MAC-BC with relays.

- Uplink: Fixed-point method

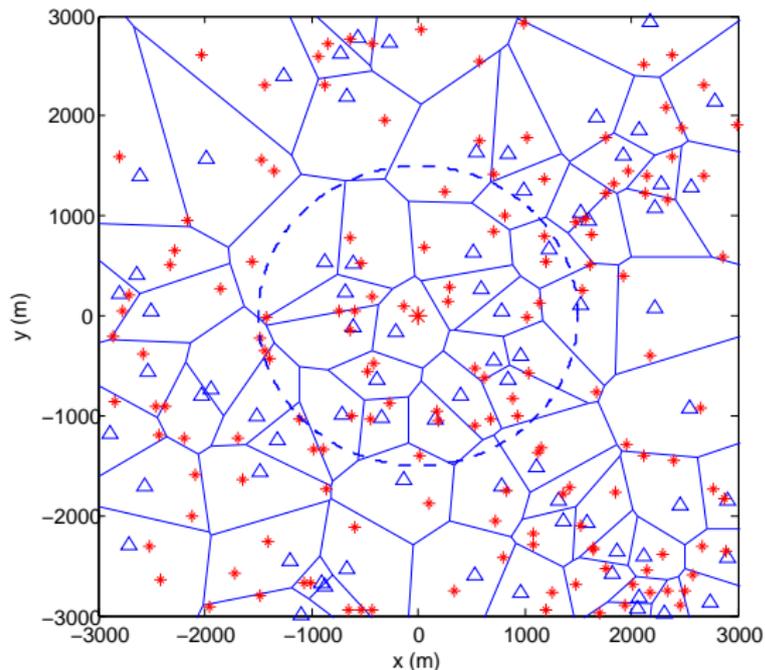
$$\begin{aligned} & \underset{\{p_i^{\text{ul}}, \mathbf{w}_i\}, \{q_l^{\text{ul}}\}}{\text{minimize}} && P^{\text{ul}}(\{p_i^{\text{ul}}\}) \\ & \text{subject to} && R_k^{\text{ul}}(\{p_i^{\text{ul}}, \mathbf{w}_i\}, \{q_l^{\text{ul}}\}) \geq R_k, \quad \forall k, \\ & && C_l^{\text{ul}}(\{p_i^{\text{ul}}\}, q_l^{\text{ul}}) \leq C_l, \quad \forall l. \end{aligned}$$

- Downlink: Based on uplink solution

$$\begin{aligned} & \underset{\{p_i^{\text{dl}}, \mathbf{v}_i\}, \{q_l^{\text{dl}}\}}{\text{minimize}} && P^{\text{dl}}(\{p_i^{\text{dl}}\}, \{q_l^{\text{dl}}\}) \\ & \text{subject to} && R_k^{\text{dl}}(\{p_i^{\text{dl}}, \mathbf{v}_i\}, \{q_l^{\text{dl}}\}) \geq R_k, \quad \forall k, \\ & && C_l^{\text{dl}}(\{p_i^{\text{dl}}, \mathbf{v}_i\}, q_l^{\text{dl}}) \leq C_l, \quad \forall l. \end{aligned}$$

Performance Analysis of C-RAN

- Achievable rates in C-RAN are significantly influenced by:
 - Distances between transmitters and receivers.
 - Random channel fading realizations.
- Stochastic geometry provides analytic tool [Andrews-Bacelli-Ganti'11]



Obtaining signal and interference distributions is the main challenge!

- Model distance-dependent channel characterization:

$$g_{ilmj} = \sqrt{\beta_{ilmj}} h_{ilmj} \text{ with } h_{ilmj} \sim \mathcal{CN}(0, \mathbf{I}_M), \beta_{ilmj} = \left(1 + \frac{r_{ilmj}}{d_0}\right)^{-\alpha}$$

- Approximate signal and interference distributions as Gamma distributions with modified parameters [Heath-Wu-Kwon-Soong'11]

$$\mathbf{g}_{il}^H \mathbf{g}_{il} = \sum_{b=1}^{B_l} \beta_{ilbl} h_{ilbl}^H h_{ilbl} \sim \Gamma(k_{il}, \theta_{il})$$

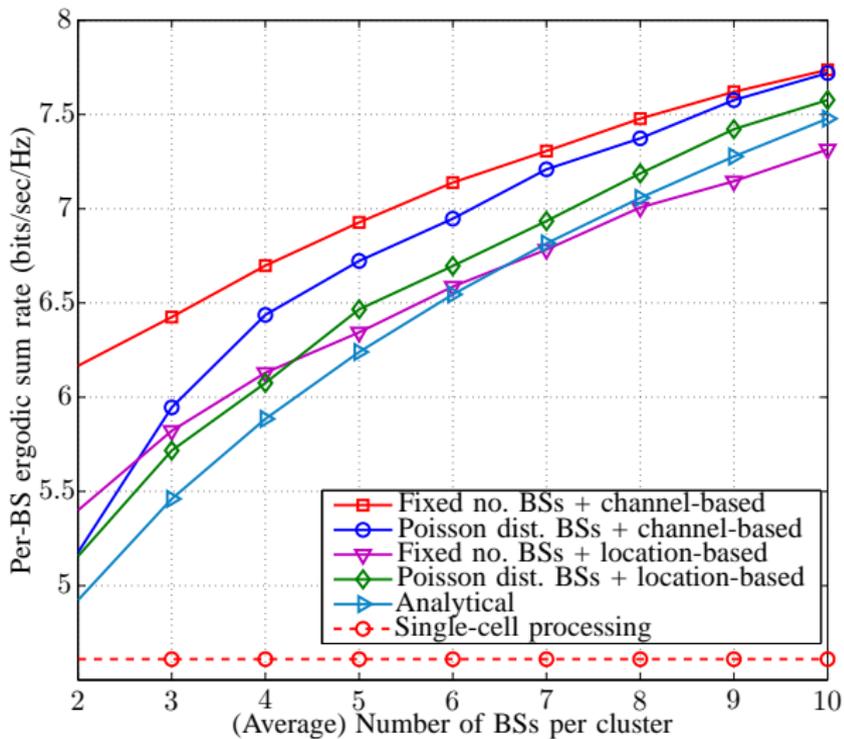
$$\text{where } k_{il} = M \frac{\left(\sum_{b=1}^{B_l} \beta_{ilbl}\right)^2}{\sum_{b=1}^{B_l} \beta_{ilbl}^2}, \quad \theta_{il} = \frac{\sum_{b=1}^{B_l} \beta_{ilbl}^2}{\sum_{b=1}^{B_l} \beta_{ilbl}}$$

- Key fact:

$$\ln(1+x) = \int_0^{\infty} \frac{e^{-z}}{z} (1 - e^{-xz}) dz$$

Ergodic rate can be characterized in terms of Laplace transforms!

How Large Should the Cluster Size Be?



Cluster sizes are limited by the fronthaul and by CSI acquisition.

- Cloud radio-access network is an enabling architecture that allows
 - Joint signal processing across the RRHs;
 - Advanced network optimization.
- Network-wide optimization is likely to be done in the cloud.
- Summary of results in this talk:
 - Uplink: Compression with optimized quantization levels.
 - Downlink: Message-sharing and compression are viable strategies.
 - Design: Duality, WMMSE, ℓ_1 reweighting, Succ. Convex Approx.
 - Analysis: Information theory, Optimization, Stochastic geometry.
- Future wireless cellular architecture:
 - Dense, massive, *and* cooperative.

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